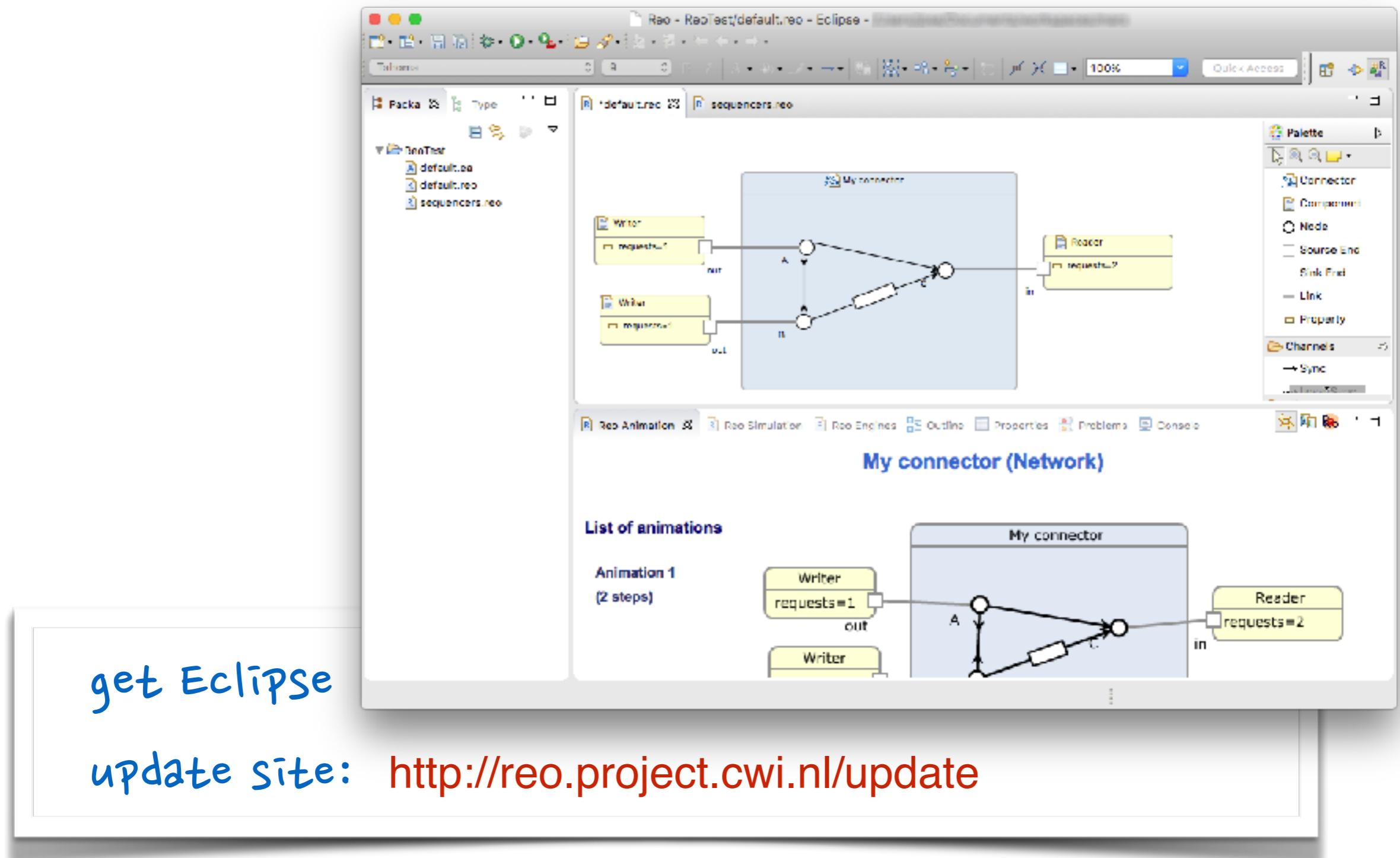


# Architectural design: the coordination perspective

José Proença  
HASLab - INESC TEC & UM  
Arquitectura e Cálculo 2015-16



# Reo eclipse toolset



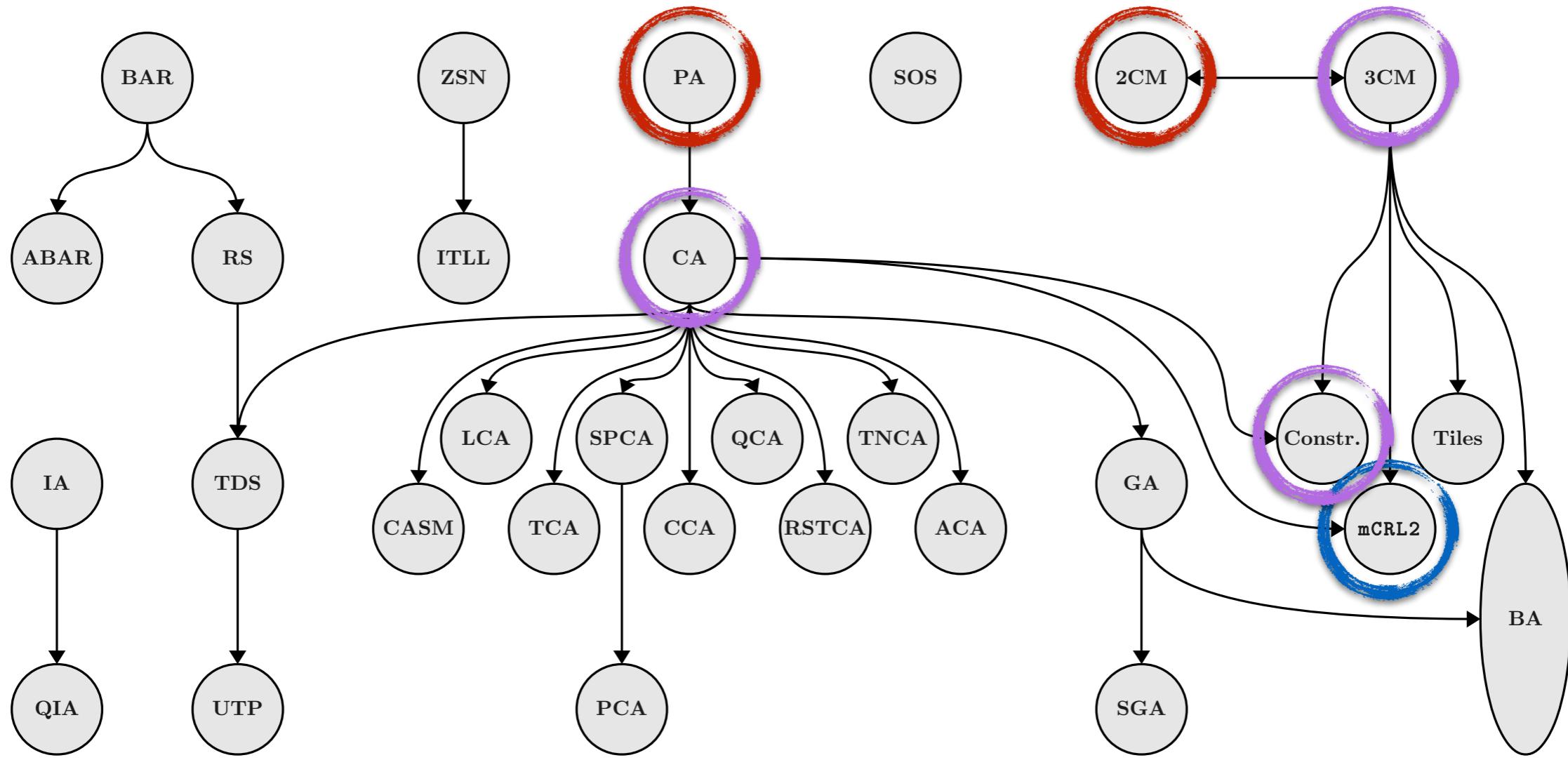
# Reo semantics

Jongmans and Arbab 2012

Overview of Thirty Semantic Formalisms for Reo

# Reo semantics

- *Coalgebraic models*
  - Timed data streams
  - Record streams
- *Coloring models*
  - **Two colors**
  - **Three colors**
  - Tile models
- *Other models*
  - **Process algebra**
  - **Constraints**
  - Petri nets & intuitionistic logic
  - Unifying theories of programming
  - Structural operational semantics
- *Operational models*
  - **Constraint automata**
  - Variants of constraint automata
    - **Port automata**
    - Timed Probabilistic
    - Continuous-time
    - Quantitative
    - Resource-sensitive timed
    - Transactional
  - Context-sensitive automata
    - Büchi automata
    - Reo automata
    - Intentional automata
    - Action constraint automata
    - Behavioral automata
  - Structural operational semantics

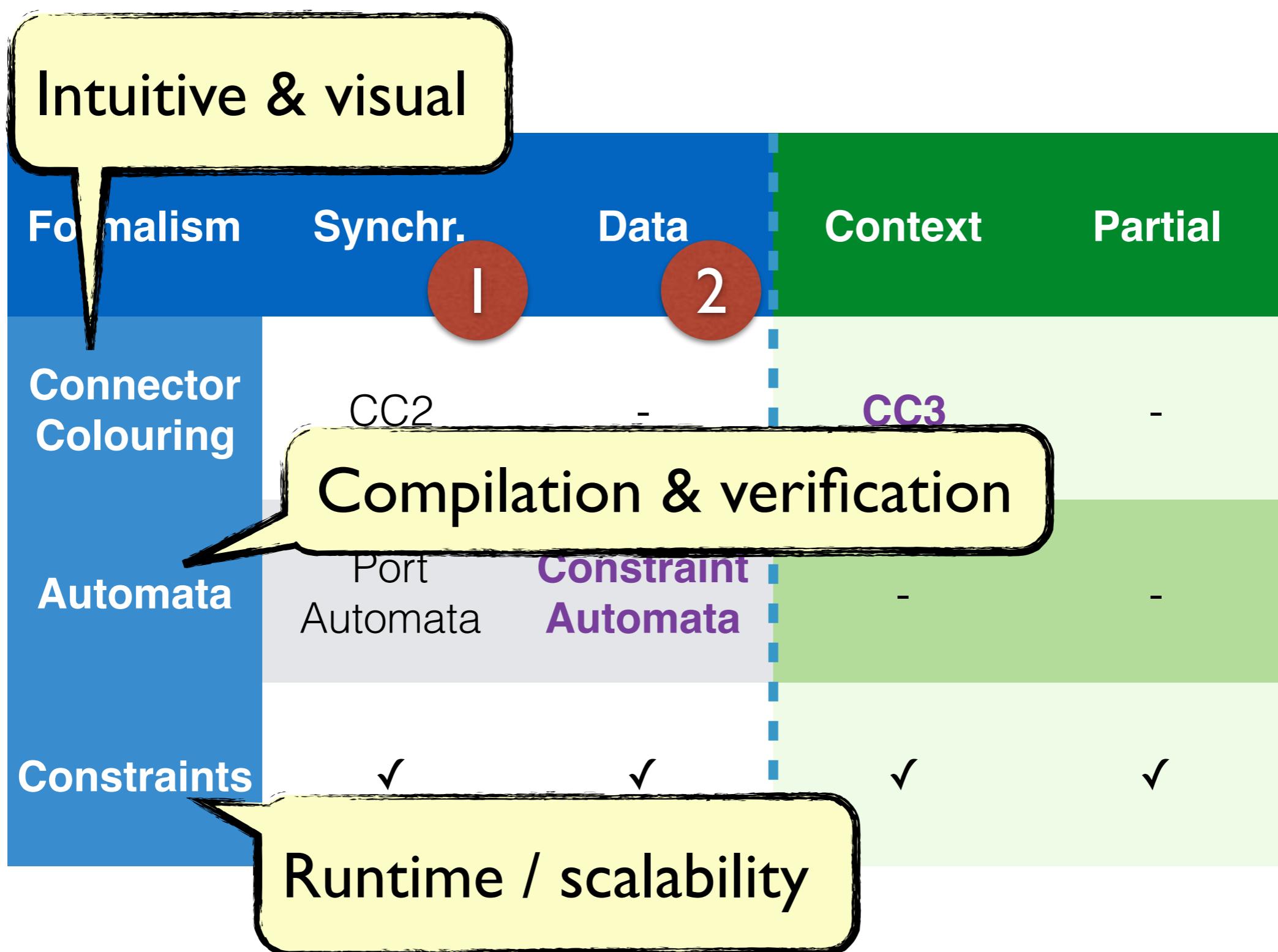


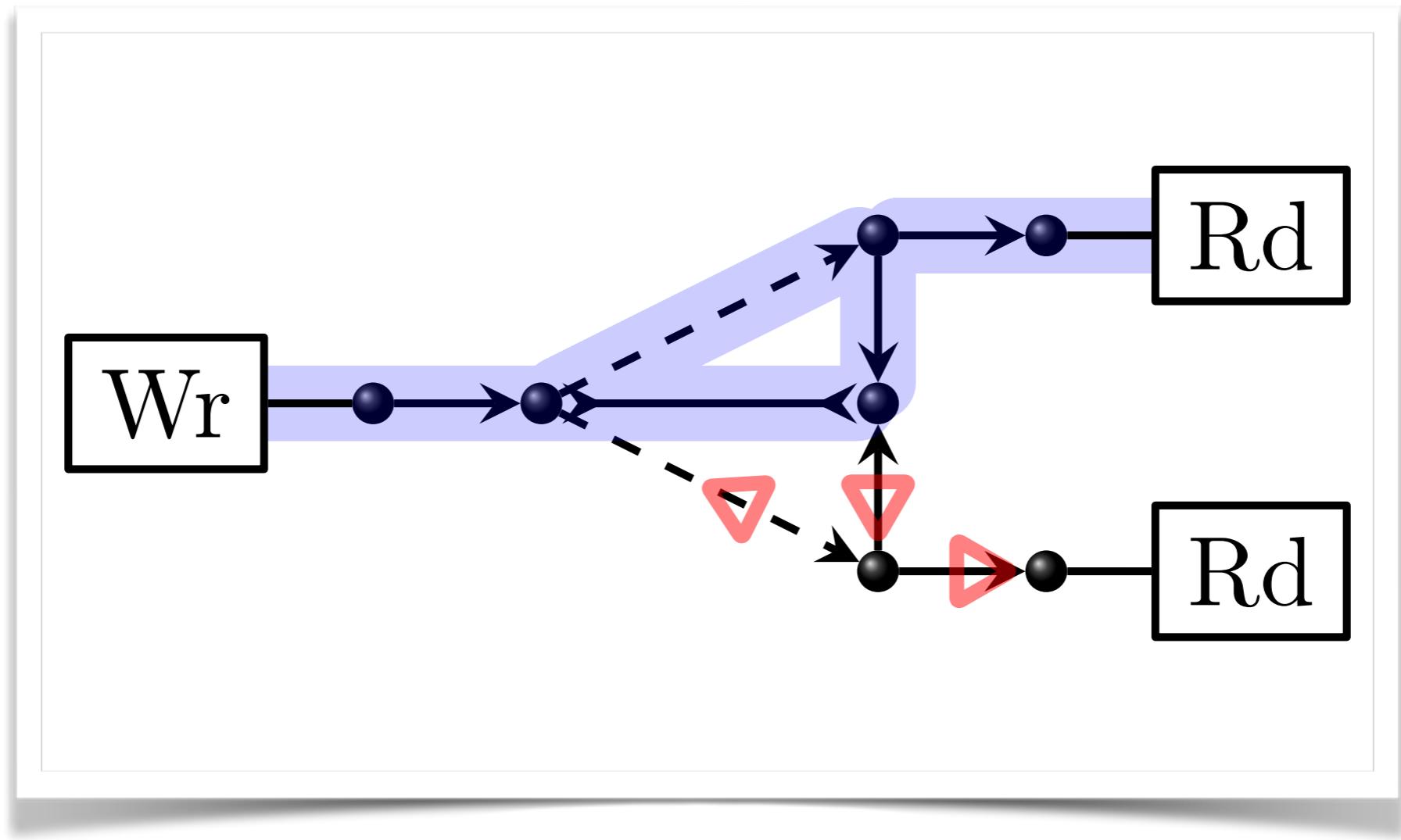
- |                |  |              |   |
|----------------|--|--------------|---|
| <b>2CM</b>     | : Coloring models with two colors [28, 29, 33]   | <b>PA</b>    | : Port automata [45]                        |
| <b>3CM</b>     | : Coloring models with three colors [28, 29, 33] | <b>PCA</b>   | : Probabilistic CA [15]                     |
| <b>ABAR</b>    | : Augmented BAR [39, 40]                         | <b>QCA</b>   | : Quantitative CA [12, 53]                  |
| <b>ACA</b>     | : Action CA [46]                                 | <b>QIA</b>   | : Quantitative IA [13]                      |
| <b>BA</b>      | : Behavioral automata [61]                       | <b>RS</b>    | : Record streams [38, 40]                   |
| <b>BAR</b>     | : Büchi automata of records [38, 40]             | <b>RSTCA</b> | : Resource-sensitive timed CA [51]          |
| <b>CA</b>      | : Constraint automata [10, 17]                   | <b>SGA</b>   | : Stochastic GA [56, 57]                    |
| <b>CASM</b>    | : CA with state memory [60]                      | <b>SOS</b>   | : Structural operational semantics [58]     |
| <b>CCA</b>     | : Continuous-time CA [18]                        | <b>SPCA</b>  | : Simple PCA [15]                           |
| <b>Constr.</b> | : Propositional constraints [30, 31, 32]         | <b>TCA</b>   | : Timed CA [8, 9]                           |
| <b>GA</b>      | : Guarded automata [20, 21]                      | <b>TDS</b>   | : Timed data streams [4, 5, 14, 62]         |
| <b>IA</b>      | : Intentional automata [33]                      | <b>Tiles</b> | : Tile models [11]                          |
| <b>ITLL</b>    | : Intuitionistic temporal linear logic [27]      | <b>TNCA</b>  | : Transactional CA [54]                     |
| <b>LCA</b>     | : Labeled CA [44]                                | <b>UTP</b>   | : Unifying theories of programming [55, 52] |
| <b>mCRL2</b>   | : Process algebra [47, 48, 49]                   | <b>ZSN</b>   | : Zero-safe nets [27]                       |

# Outline

Formalism	Synchr.	Data	Context	Partial
Connector Colouring	CC2	-	CC3	-
Automata	Port Automata	<b>Constraint Automata</b>	-	-
Constraints	✓	✓	✓	✓

# Outline

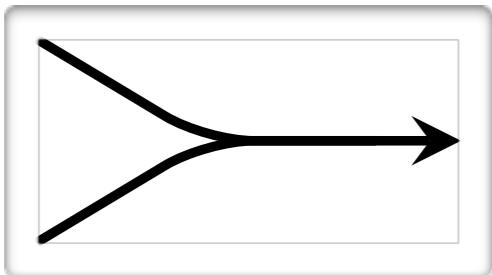




# Reo Connector Colouring

Dave Clarke, David Costa, and Farhad Arbab. Connector colouring I: Synchronisation and context dependency

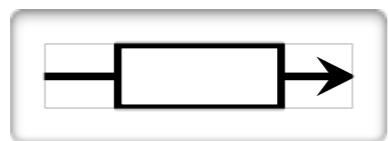
# Behaviour?



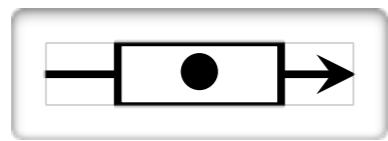
merger: data flows from one of the source ends to the sink end



lossy-sync: either data flows from the source to the sink end, OR it is lost

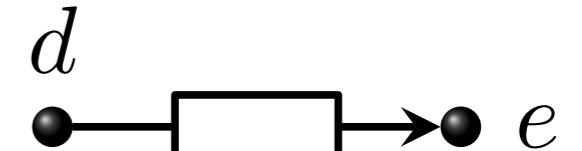
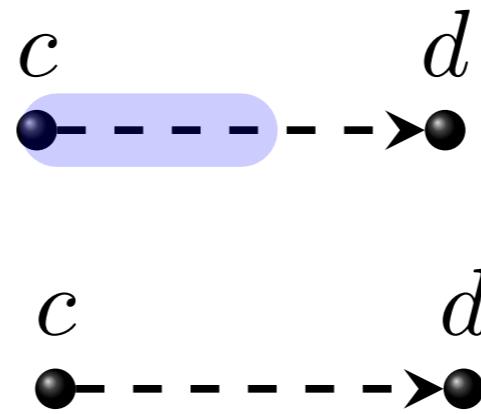
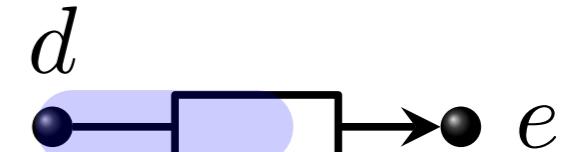
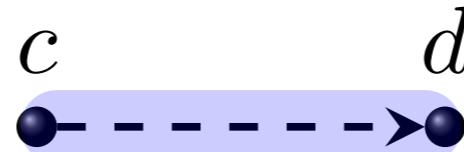
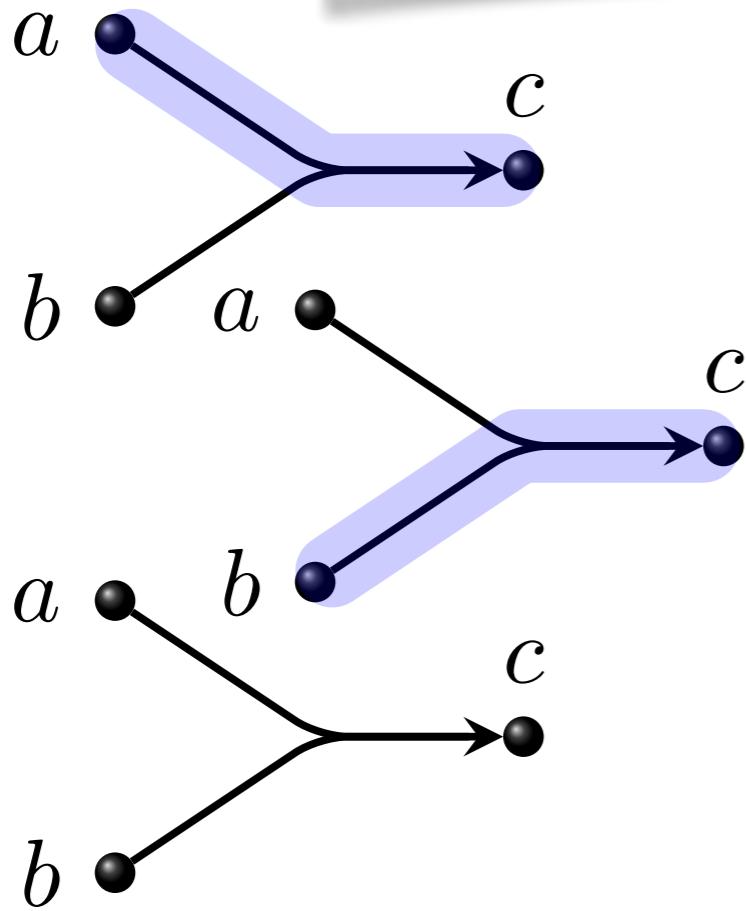
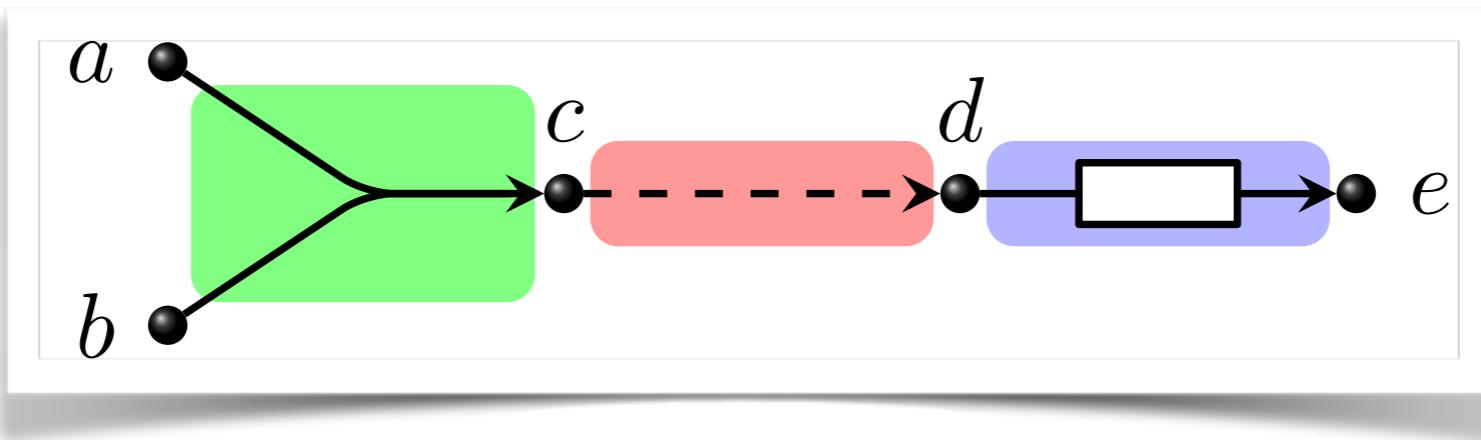


FIFO-1: data flows from the source end to the buffer, becoming a FIFOFull-1

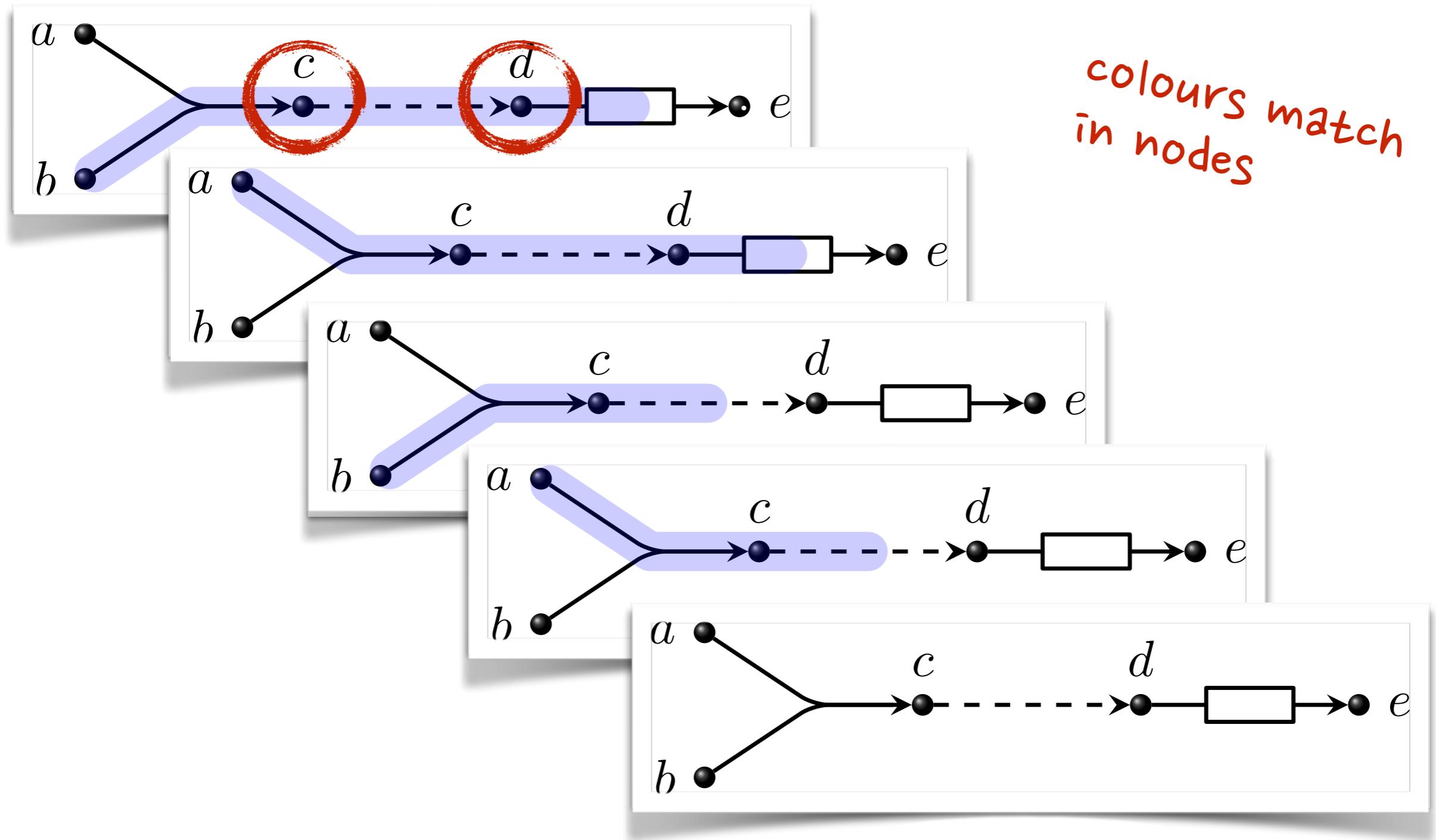


FIFOFull-1: data flows from the buffer to the sink buffer, becoming a FIFO-1

# Colourings to describe synchronous dataflow

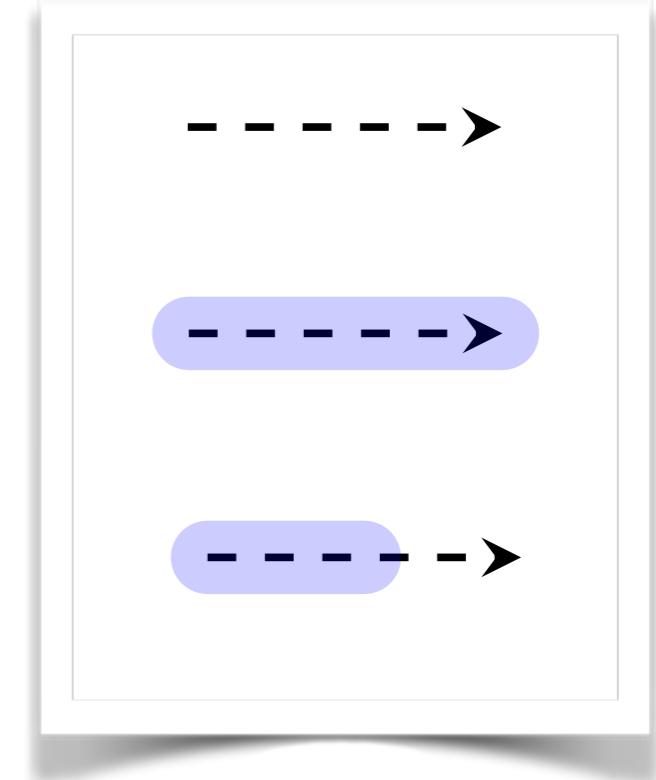


# Colouring composition



# Colouring semantics (CC2)

- *Colouring*:  $\text{End} \rightarrow \{\text{Flow}, \text{NoFlow}\}$
- *Colouring table*:  $\text{Set}(\text{Colouring})$
- *Composition* = matching colours
- More visual (intuitive)
- Used for generating animations



# Colouring semantics (CC2)

- *Colouring*:  $\text{End} \rightarrow \{\text{Flow}, \text{NoFlow}\}$
- *Colouring table*:  $\text{Set}(\text{Colouring})$
- *Composition* = matching colours

----->

----->

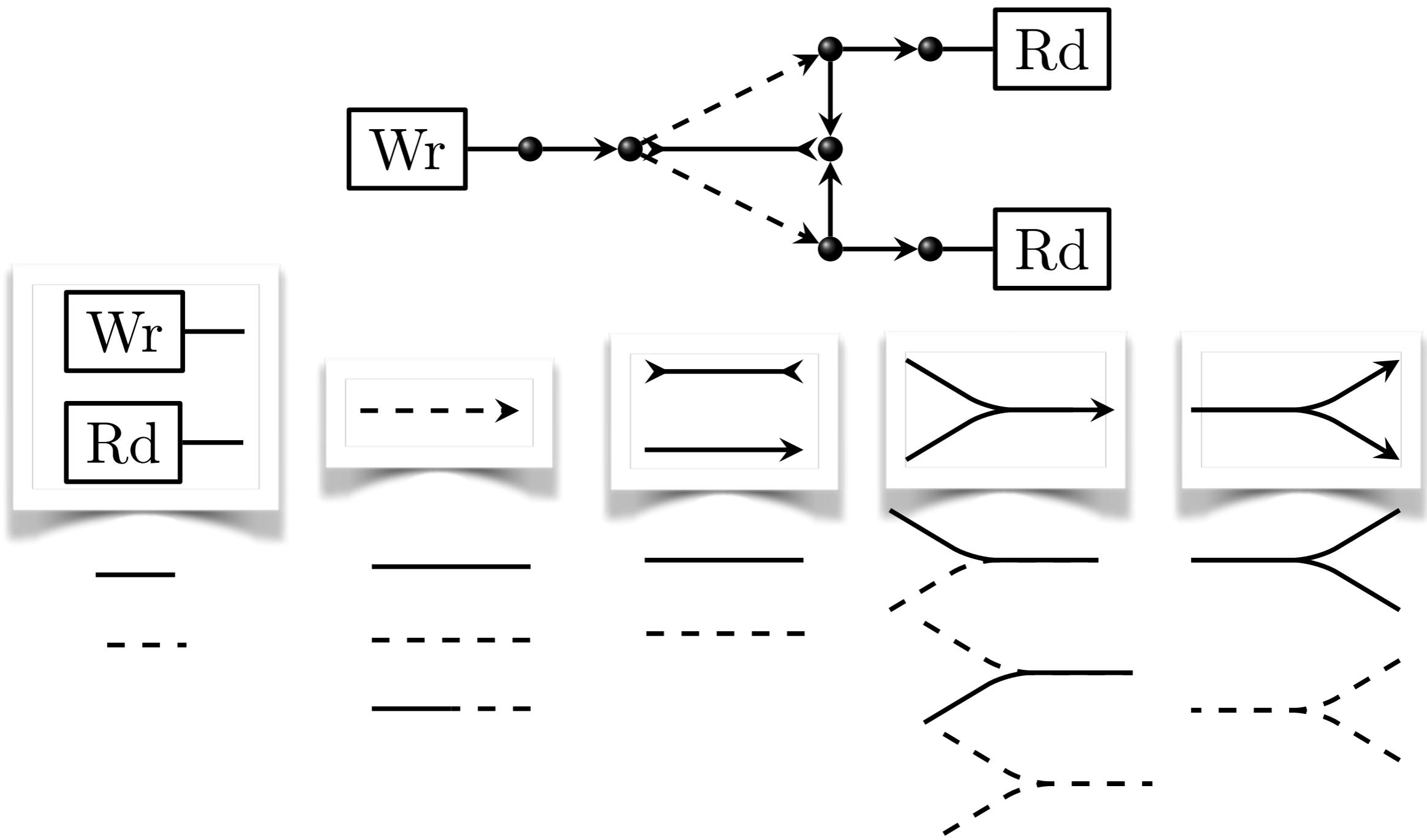
$$CT_1 \bowtie CT_2 =$$

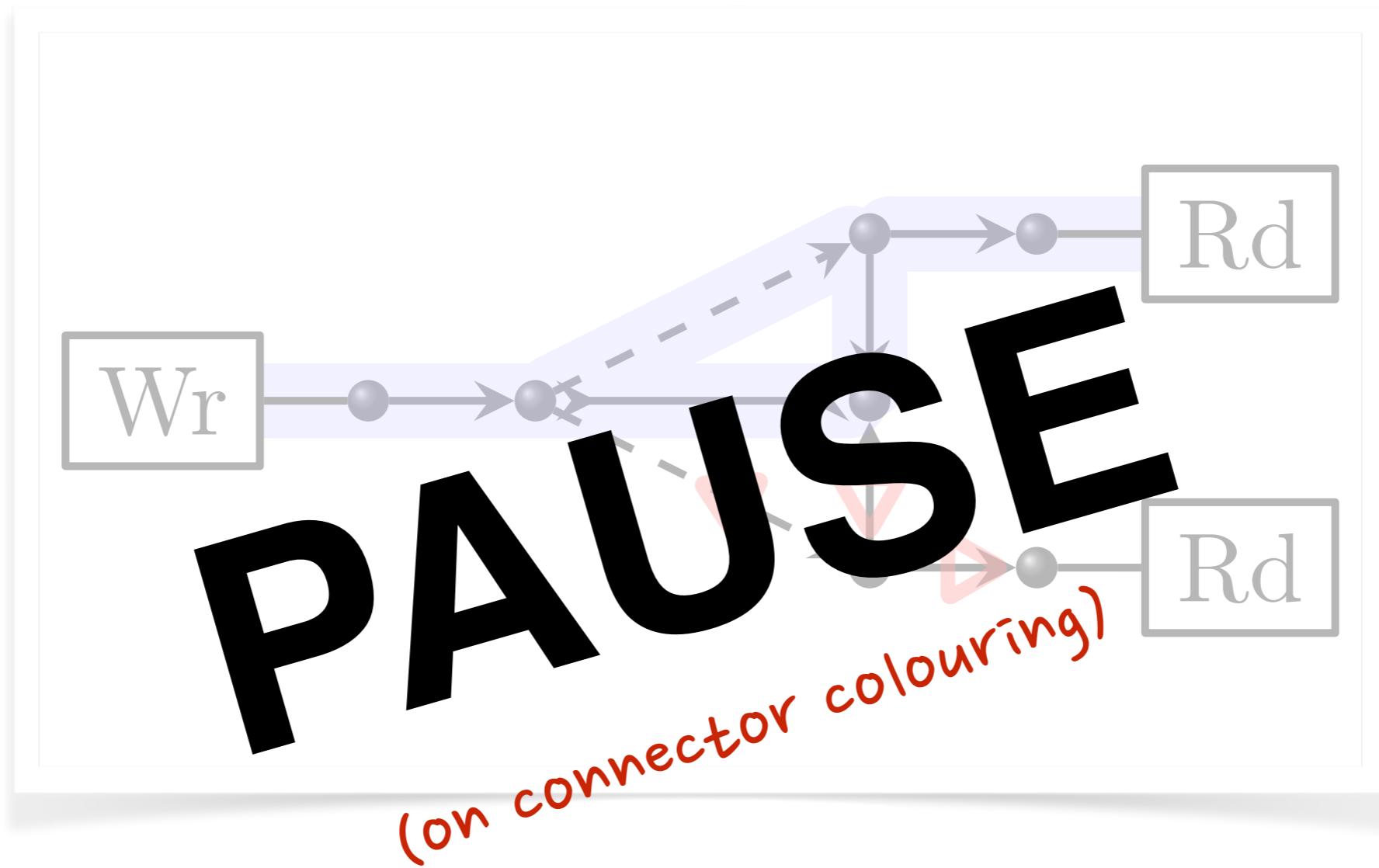
$$\{cl_1 \bowtie cl_2 \mid cl_1 \in CT_1, cl_2 \in CT_2, cl_1 \frown cl_2\}$$

$$cl_1 \frown cl_2 = \forall e \in \text{dom}(cl_1) \cap \text{dom}(cl_2) \cdot cl_1(e) = cl_2(e)$$

$$cl_1 \bowtie cl_2 = cl_1 \cup cl_2$$

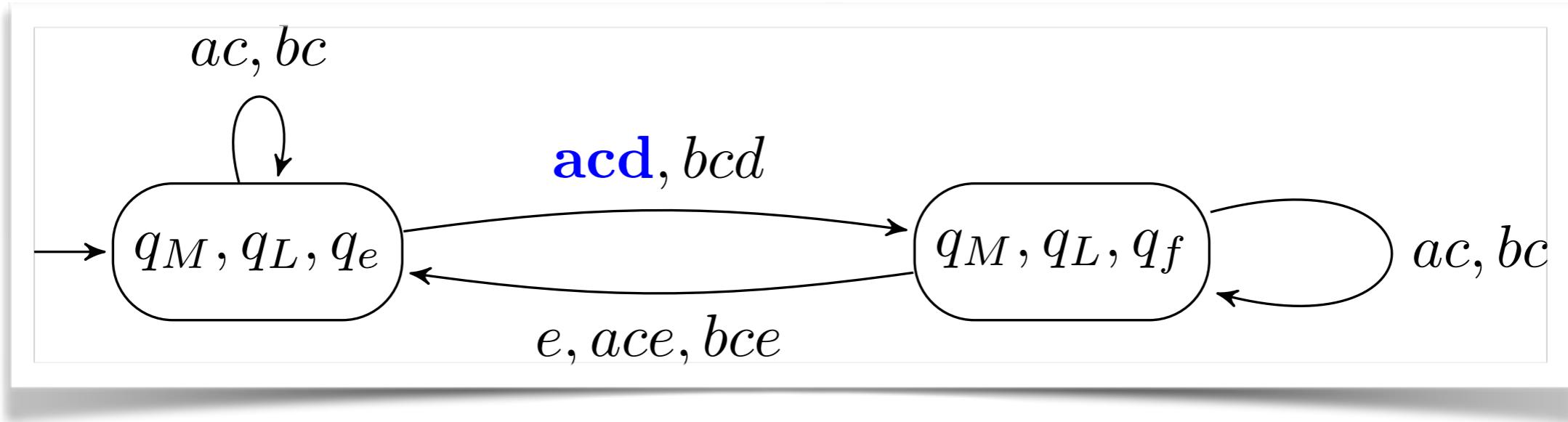
# Exercise: compose colouring tables





# Reo Connector Colouring

Dave Clarke, David Costa, and Farhad Arbab. Connector colouring I: Synchronisation and context dependency



# Port and Constraint Automata

Christel Baier, Marjan Sirjani, Farhad Arbab, Jan Rutten. Modeling Component Connectors in Reo by Constraint Automata. 2004

Christian Koehler and Dave Clarke. Decomposing Port Automata. 2009

# Connector behaviour (statefull)

- Dataflow behaviour is **discrete** in time: it can be observed and snapshots taken at a pace fast enough to obtain (at least) a snapshot as often as the configuration of the connector changes
- At each time unit the connector performs an **evaluation step**: it evaluates its configuration and according to its interaction constraints changes to another (possibly different) configuration
- A connector can **fire multiple ports in the same evaluation step**

# Port Automata

$$\mathcal{A} = (\mathcal{Q}, \mathcal{N}, \rightarrow, \mathcal{Q}_0)$$

 $\mathcal{Q}$ 

set of states

 $\mathcal{N}$ a set of ports  $\mathcal{N}$  $\rightarrow \subseteq \mathcal{Q} \times 2^{\mathcal{N}} \times \mathcal{Q}$ 

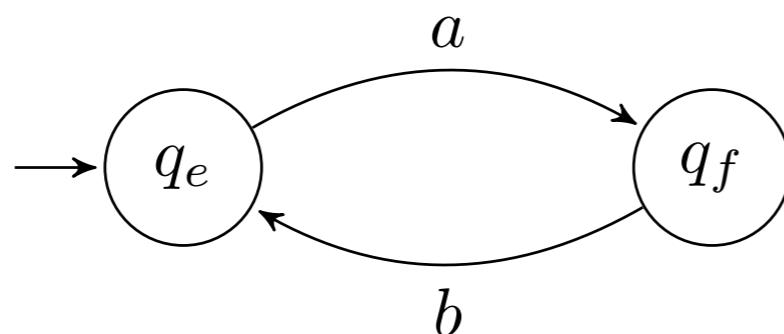
a transition relation

 $\mathcal{Q}_0 \subseteq \mathcal{Q}$ 

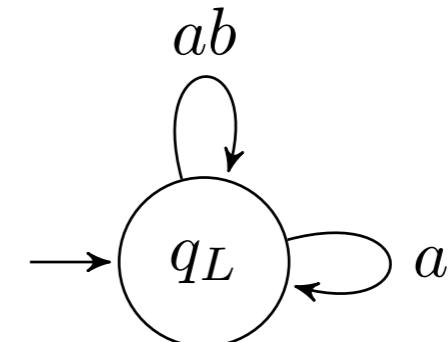
a set of initial states

transitions must have a non-empty set of ports!

examples:

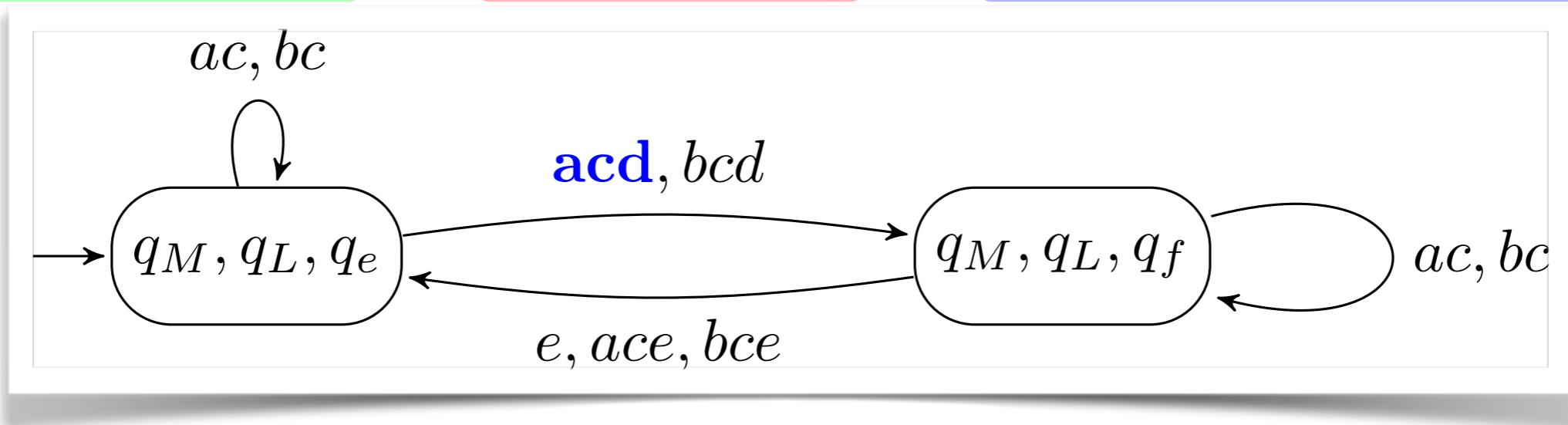
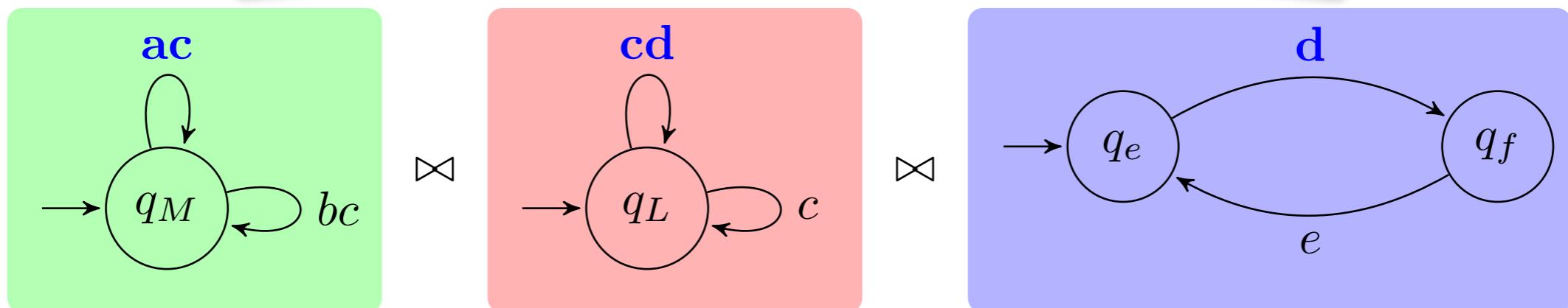
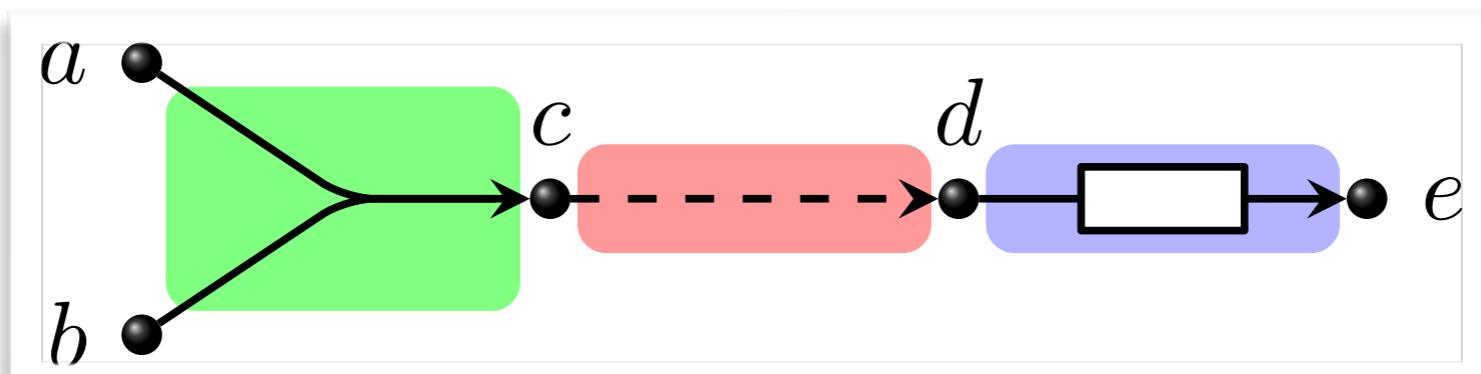


$a \xrightarrow{\quad} b$

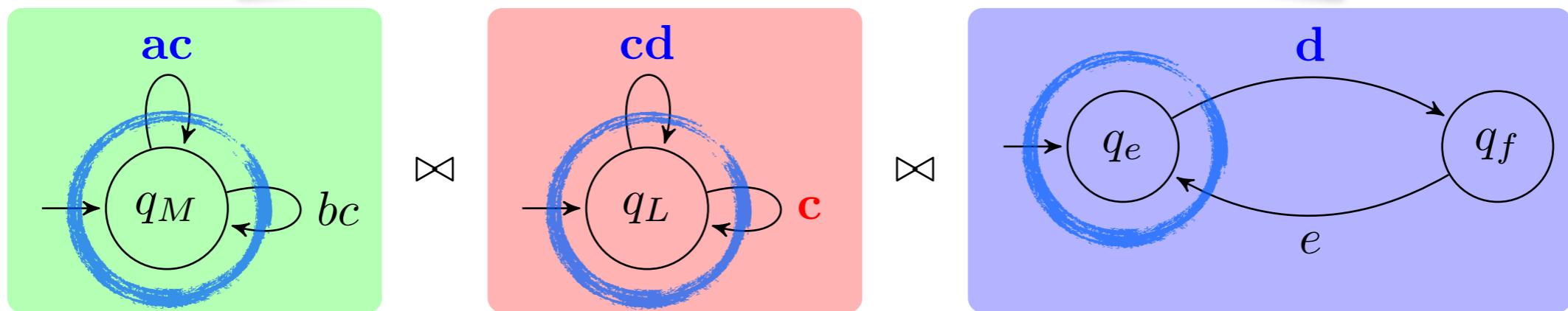
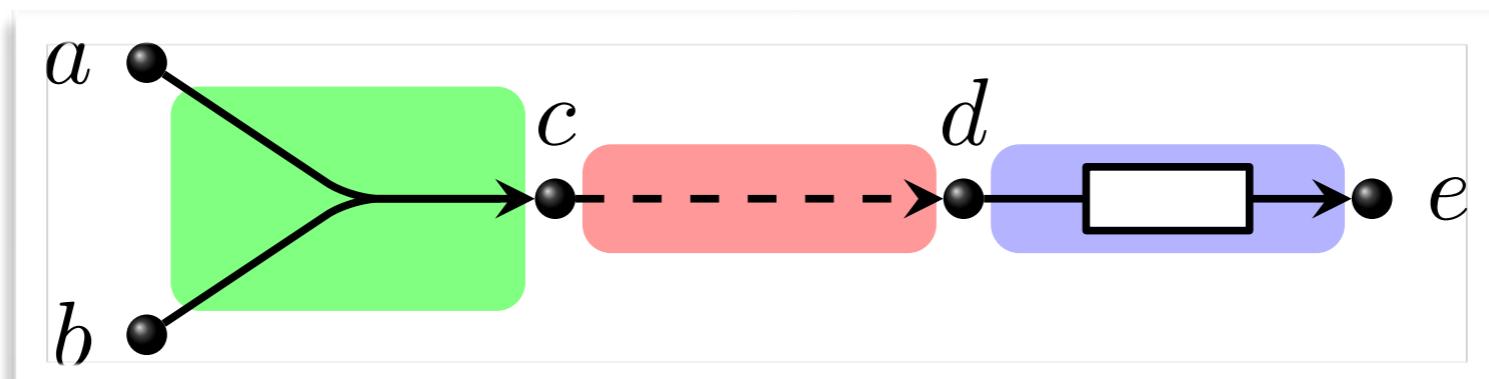


$a \dashrightarrow b$

# Composing steps



# Composing steps



$$ac \otimes cd \otimes d = acd$$

$$ac \otimes c \otimes d = \perp$$

# Composition - formally

*Definition 2.* The product of two port automata  $\mathcal{A}_1 = (\mathcal{Q}_1, \mathcal{N}_1, \rightarrow_1, \mathcal{Q}_{0,1})$  and  $\mathcal{A}_2 = (\mathcal{Q}_2, \mathcal{N}_2, \rightarrow_2, \mathcal{Q}_{0,2})$  is defined by

$$\mathcal{A}_1 \bowtie \mathcal{A}_2 = (\mathcal{Q}_1 \times \mathcal{Q}_2, \mathcal{N}_1 \cup \mathcal{N}_2, \rightarrow, \mathcal{Q}_{0,1} \times \mathcal{Q}_{0,2})$$

where  $\rightarrow$  is defined by the rule

$$\frac{q_1 \xrightarrow{N_1} p_1 \quad q_2 \xrightarrow{N_2} p_2 \quad N_1 \cap \mathcal{N}_2 = N_2 \cap \mathcal{N}_1}{\langle q_1, q_2 \rangle \xrightarrow{N_1 \cup N_2} \langle p_1, p_2 \rangle}$$

and the following and its symmetric rule

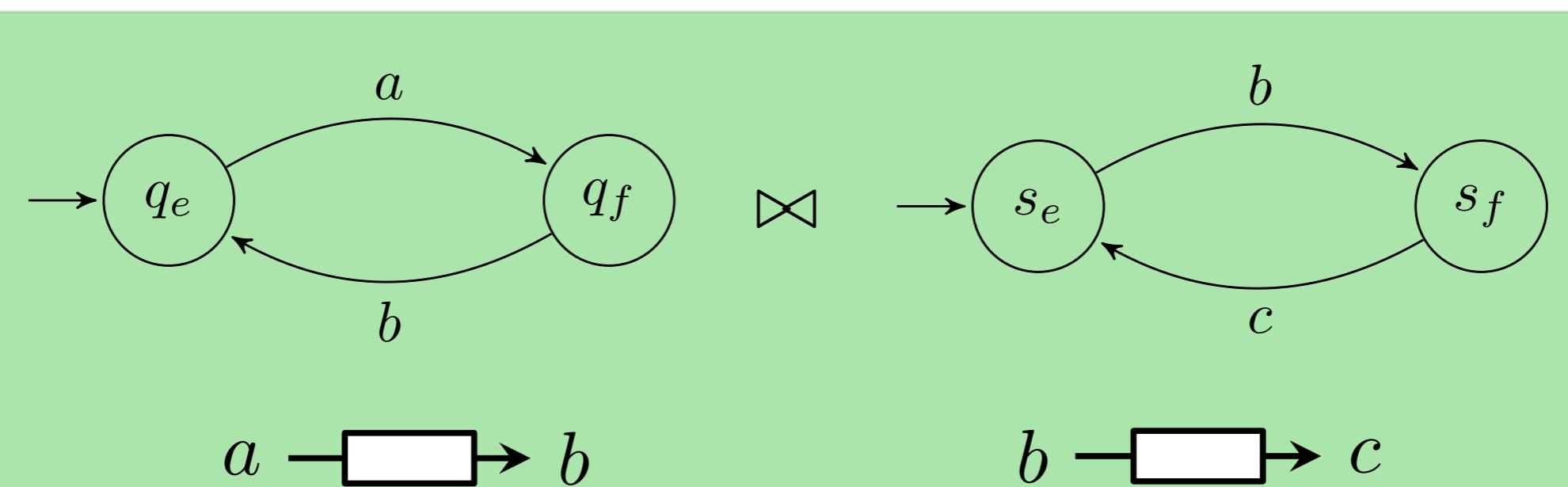
$$\frac{q_1 \xrightarrow{N_1} p_1 \quad N_1 \cap \mathcal{N}_2 = \emptyset}{\langle q_1, q_2 \rangle \xrightarrow{N_1} \langle p_1, q_2 \rangle}$$

# Formalize and compose

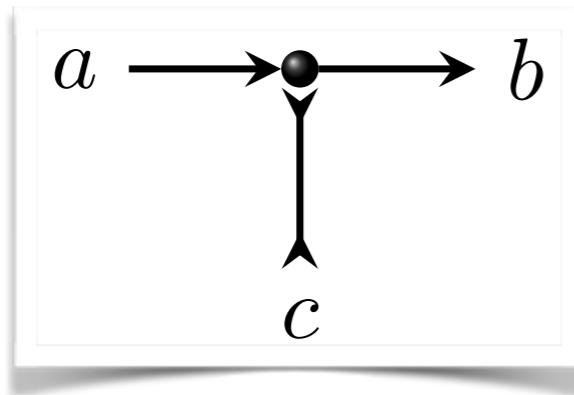
$$\frac{q_1 \xrightarrow{N_1} p_1 \quad q_2 \xrightarrow{N_2} p_2 \quad N_1 \cap \mathcal{N}_2 = N_2 \cap \mathcal{N}_1}{\langle q_1, q_2 \rangle \xrightarrow{N_1 \cup N_2} \langle p_1, p_2 \rangle}$$

$$\mathcal{A} = (\mathcal{Q}, \mathcal{N}, \rightarrow, \mathcal{Q}_0)$$

$$\frac{q_1 \xrightarrow{N_1} p_1 \quad N_1 \cap \mathcal{N}_2 = \emptyset}{\langle q_1, q_2 \rangle \xrightarrow{N_1} \langle p_1, q_2 \rangle}$$

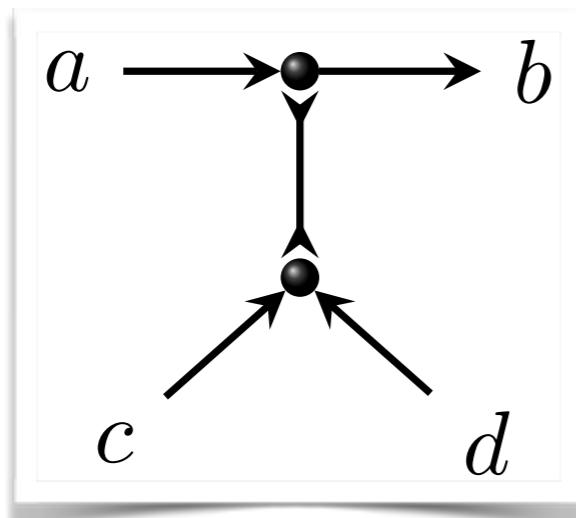


# Examples I



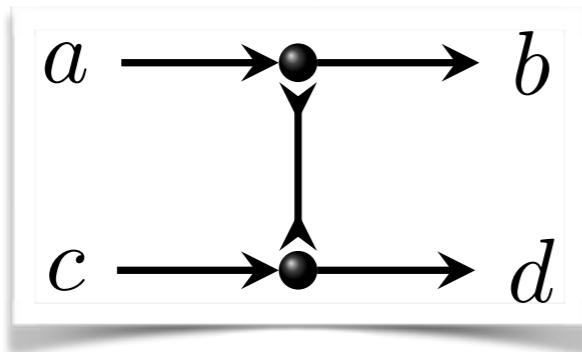
Flow regulator

“b” controls flow  
from “a” to “c”

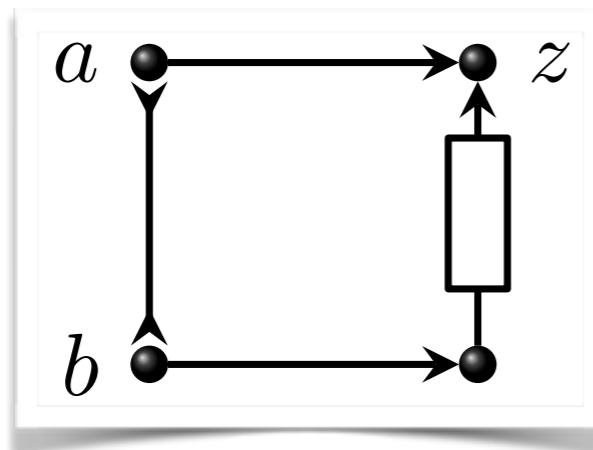


data flows from “a”  
to “b” ONLY if  
either “c” or “d”  
have data

# Examples II



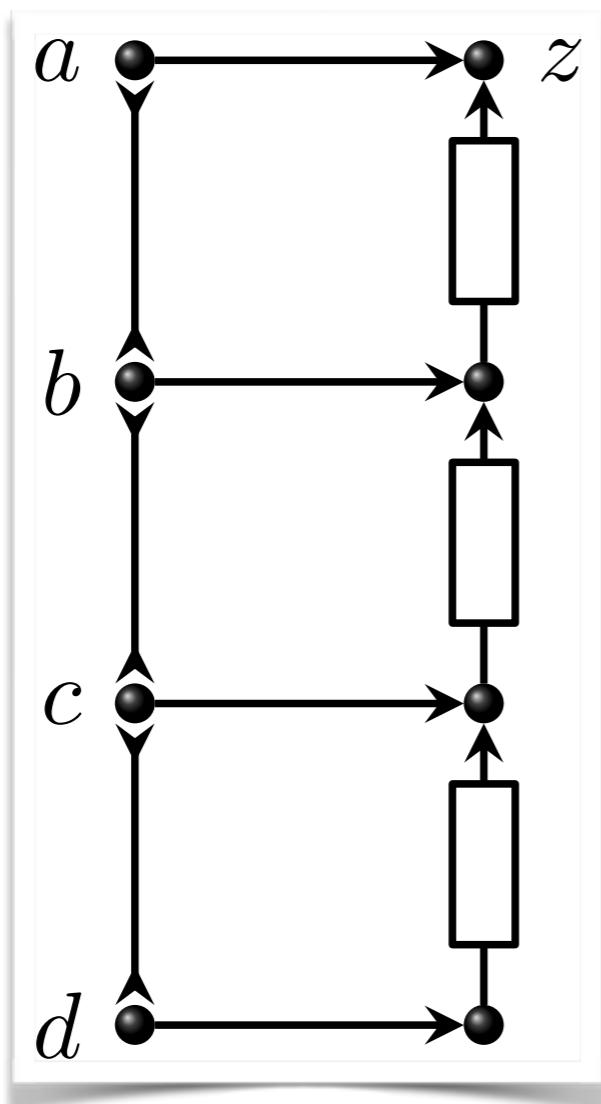
Synchronising barrier  
data flows “a”  $\rightarrow$  “b”  
IFF  
data flows “c”  $\rightarrow$  “d”



Alternator

data flows from “a”  
and from “b” to “z”,  
alternating (+ extra  
synch constraints)

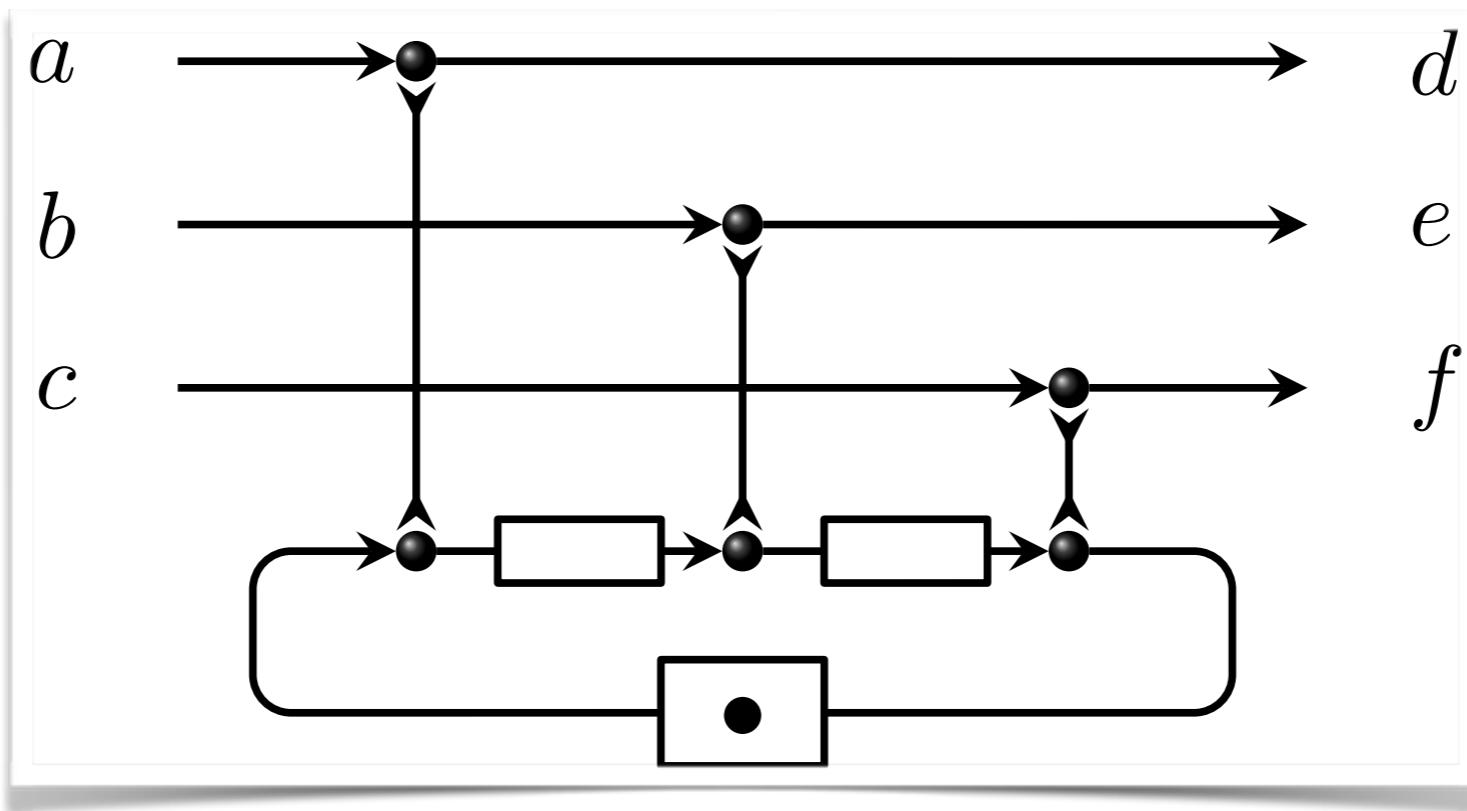
# Examples III



N-Alternator

data flows from “*a*”, “*b*”, “*c*”, and “*d*” to “*z*”, alternating (+ extra synch constraints)

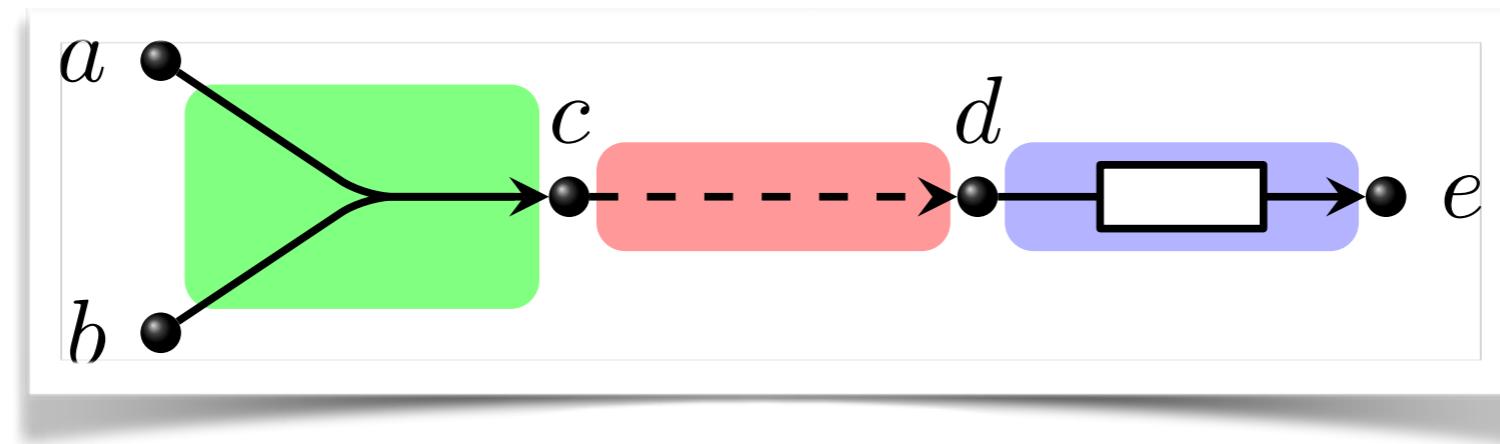
# Examples IV



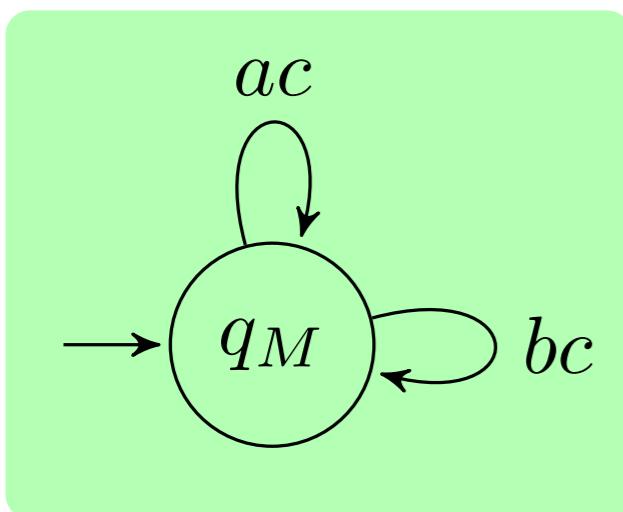
Sequencer

Data flows from "a" to "d", "b" to "e",  
and "c" to "f" alternating.

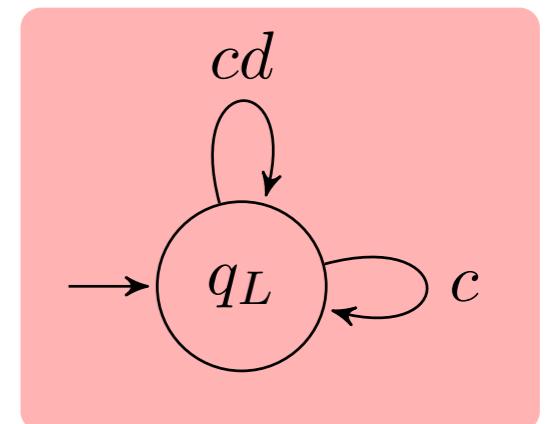
# Reo in mCRL2



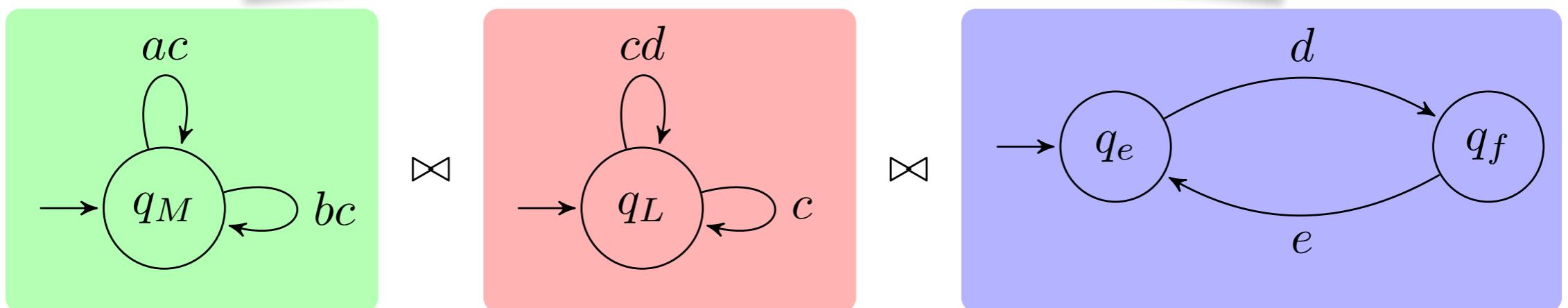
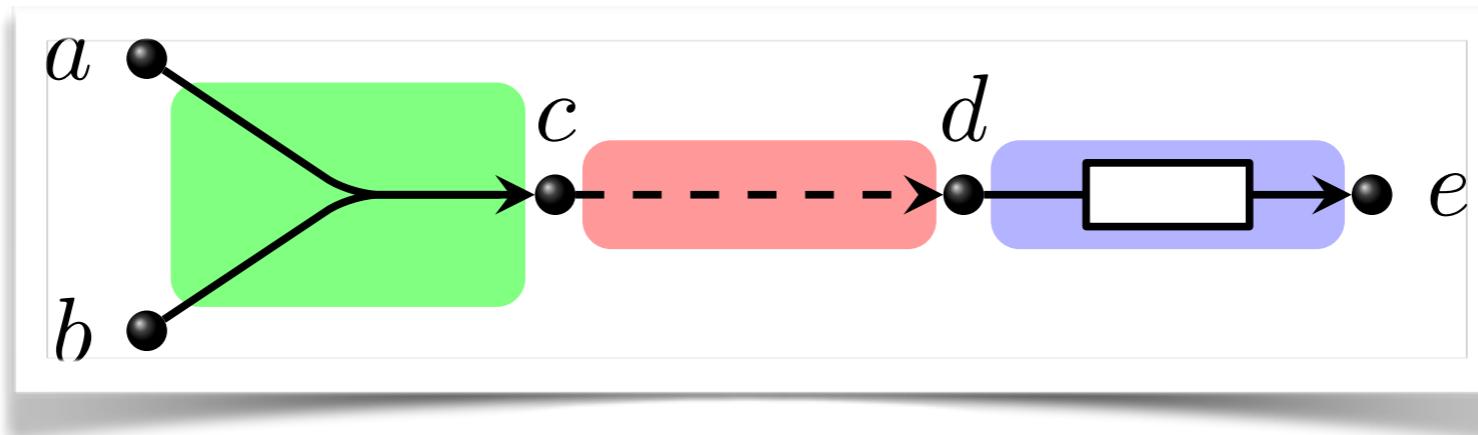
Lossy = ( $c|d + c$ ).Lossy



Merger = ( $a|c + b|c$ ).Merger

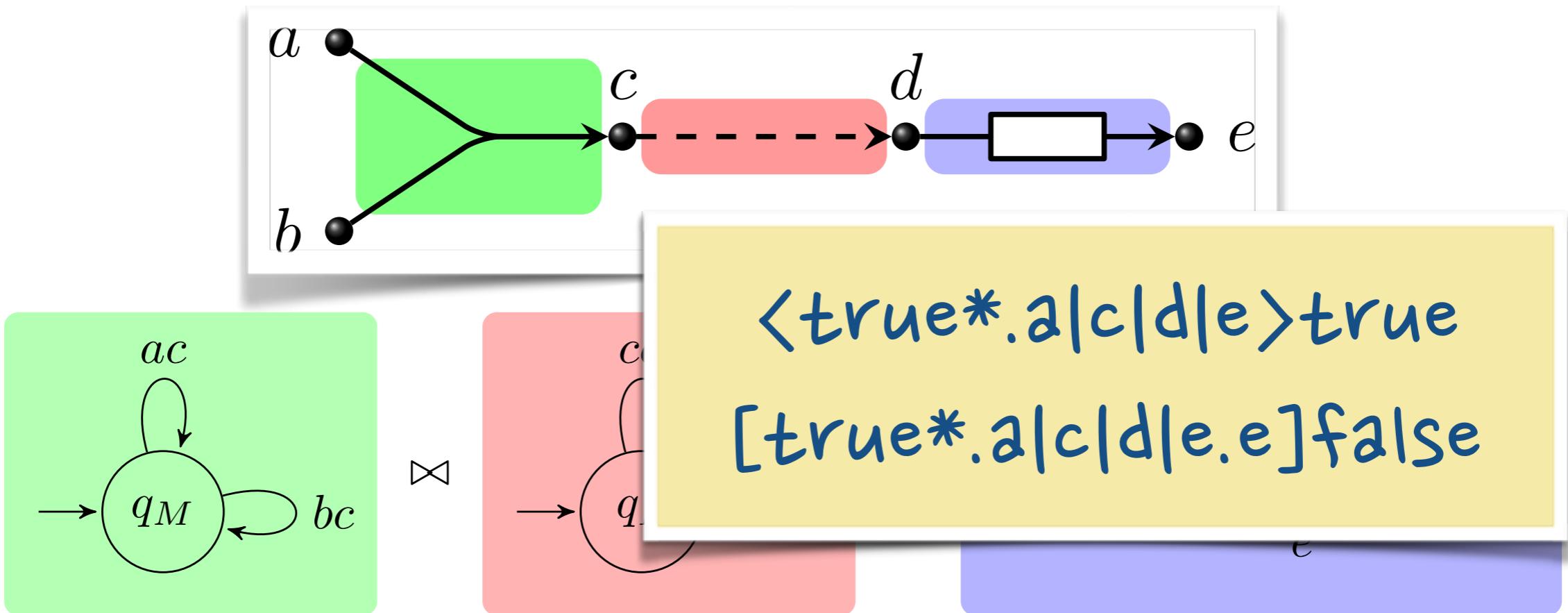


# Reo in mCRL2



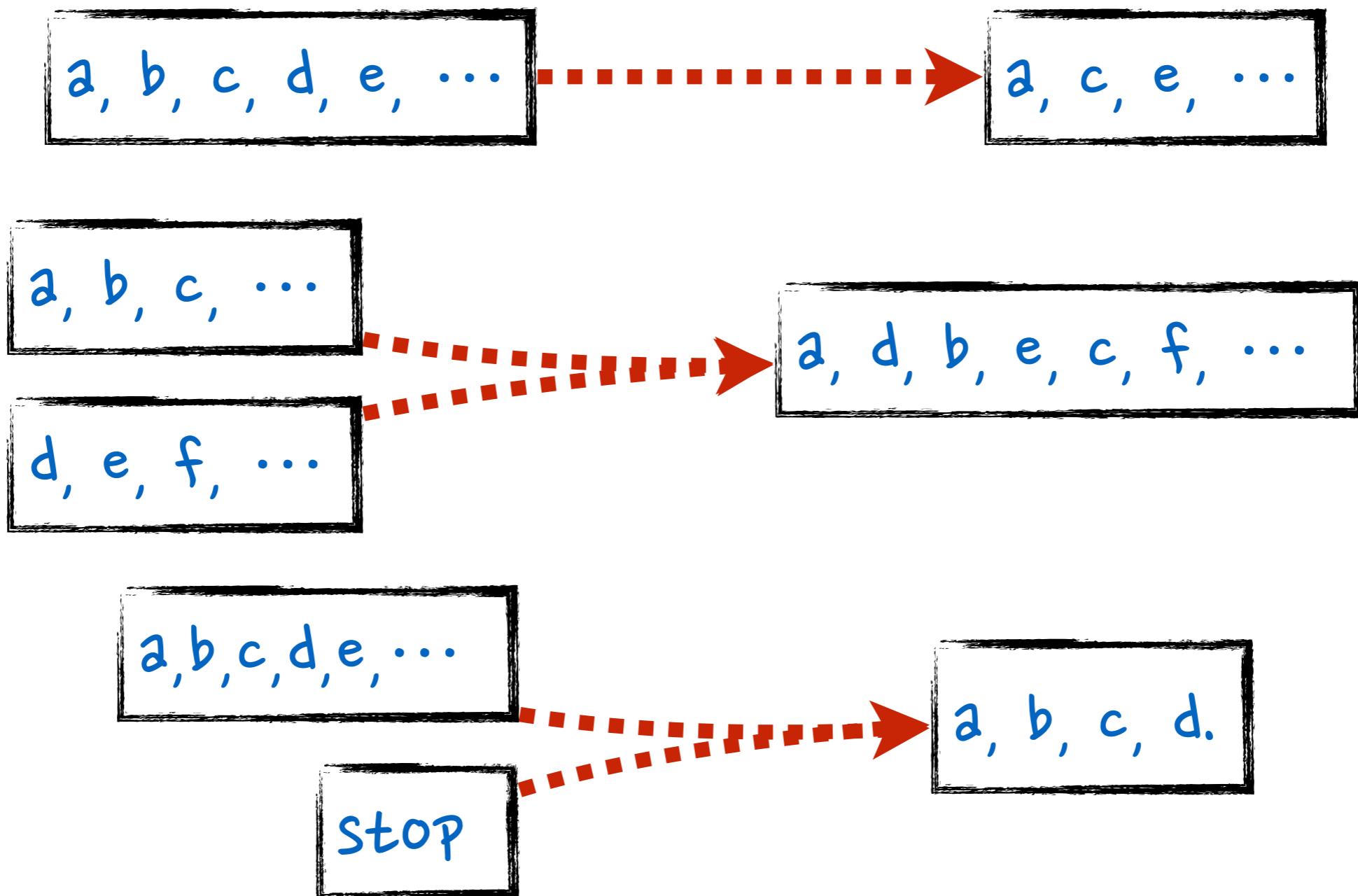
Conn = hide( $\{c, d\}$ ,  
block( $\{c_1, c_2, d_1, d_2\}$  ,  
comm( $\{c_1|c_2 \rightarrow c, d_1|d_2 \rightarrow d\}$  ,  
Merger || Lossy || FIFO1 )))

# Reo in mCRL2



Conn = hide( $\{c, d\}$ ,  
block( $\{c_1, c_2, d_1, d_2\}$  ,  
comm( $\{c_1|c_2 \rightarrow c, d_1|d_2 \rightarrow d\}$  ,  
Merger || Lossy || FIFO1 )))

# Build connectors



# Can you prove?

colourings and port automata provide equivalent semantics

$$\mathcal{A}(C_1) = (Q_1, \mathcal{N}_1, \rightarrow_1, \textcolor{red}{q_{0,1}})$$

$\mathcal{CT}(C)$  – colouring table of  $C$

$$\mathcal{A}(C_2) = (Q_2, \mathcal{N}_2, \rightarrow_2, \textcolor{red}{q_{0,2}})$$

$col(q \xrightarrow{P} q')$  – colouring associated  
to a transition

$$(\langle \textcolor{red}{q_{0,1}}, q_{0,2} \rangle \xrightarrow{P} \langle q_1, q_2 \rangle) \in \mathcal{A}(C_1) \bowtie \mathcal{A}(C_2)$$

$\Rightarrow$

$$col(\langle \textcolor{red}{q_{0,1}}, q_{0,2} \rangle \xrightarrow{P} \langle q_1, q_2 \rangle) \in \mathcal{CT}(C_1) \bowtie \mathcal{CT}(C_2)$$

# Can you prove? (more generically)

colourings and port automata provide equivalent semantics

$$\mathcal{A} = (\mathcal{Q}, \mathcal{N}, \rightarrow, \{q_0\})$$

$$(q_0 \xrightarrow{P} q) \in \mathcal{A}(C)$$

$$\Rightarrow$$

$$col(P, \mathcal{N}) \in \mathcal{CT}(C)$$

# Constraint Automata

Automata labelled by

- a **data constraint** which represents a set of data assignments to port names

$$g ::= \text{true} \mid d_A = v \mid g_1 \vee g_2 \mid \neg g$$

**Note:** other constraints, such as

$$d_A = d_B \stackrel{\text{abv}}{=} \vee_{d \in Data}(d_A = d \wedge d_B = d)$$

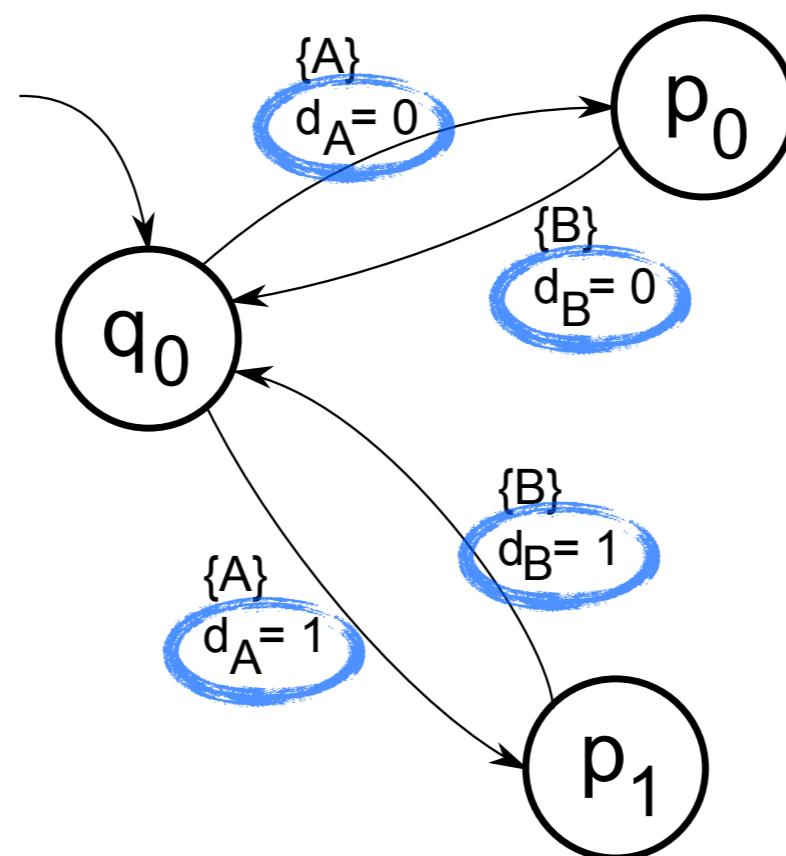
are derived.

- a **name set** which represents the set of port names at which IO can occur

States represent the configurations of the corresponding connector, while transitions encode its maximally-parallel stepwise behaviour.

# Constraint Automata

Example: FIFOI



# Constraint Automata - Definition

$$\mathcal{A} = (\mathcal{Q}, \mathcal{N}, \rightarrow, \mathcal{Q}_0)$$

$\mathcal{Q}$

set of states

$\mathcal{N}$

a set of ports  $\mathcal{N}$

$\mathcal{Q}_0 \subseteq \mathcal{Q}$

a set of initial states

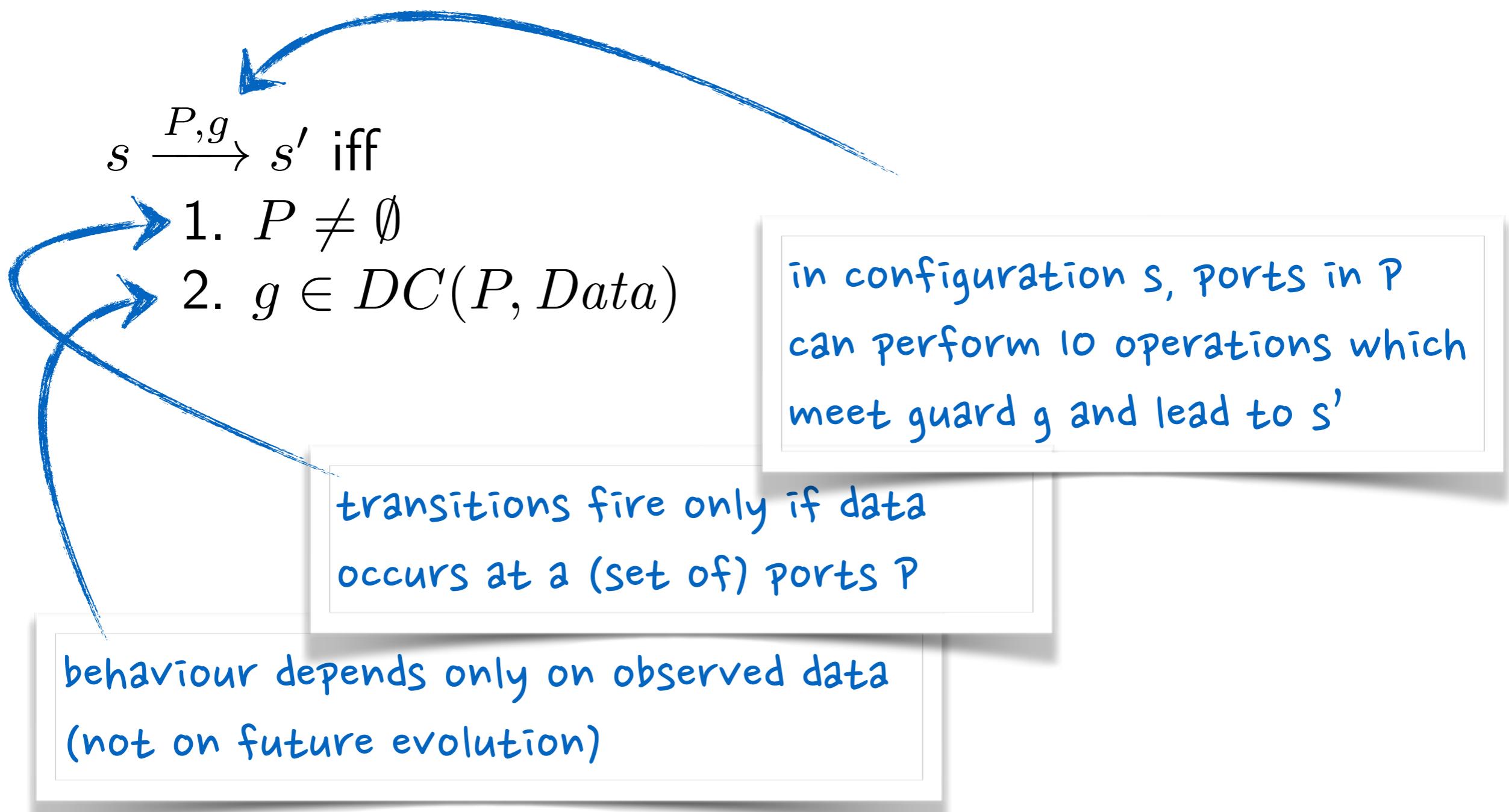
$\rightarrow \subseteq \mathcal{Q} \times 2^{\mathcal{N}} \times DC$

a transition relation such that  $\xrightarrow{P,g}$  iff

1.  $P \neq \emptyset$
2.  $g \in DC(P, Data)$

$(DC(P, Data))$  is the set of data constraints over Data and P)

# Constraint Automata - Definition

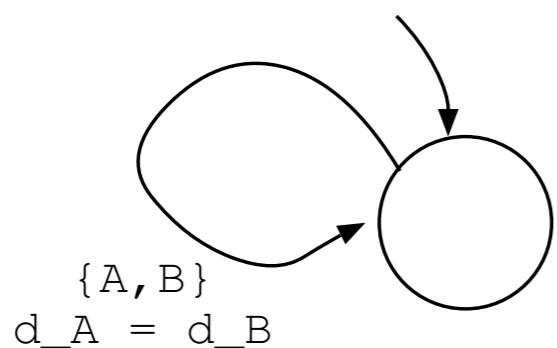


# Constraint Automata as a semantics for Reo

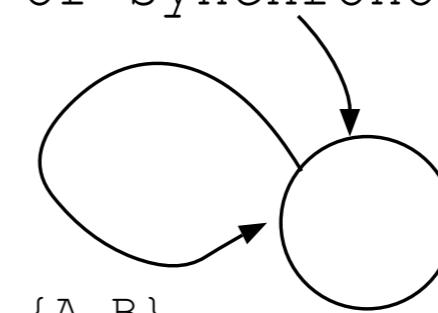
- cannot capture context-awareness [Baier, Sirjani, Arbab, Rutten 2006], but forms the basis for more elaborated models (eg, Reo automata)
- captures all behaviour alternatives of a connector; useful to generate a state-machine implementing the connector's behaviour
- basis for several tools, including the model checker Vereofy [Klappelholz, Baier 2007]

# Constraint Automata - Reo connectors

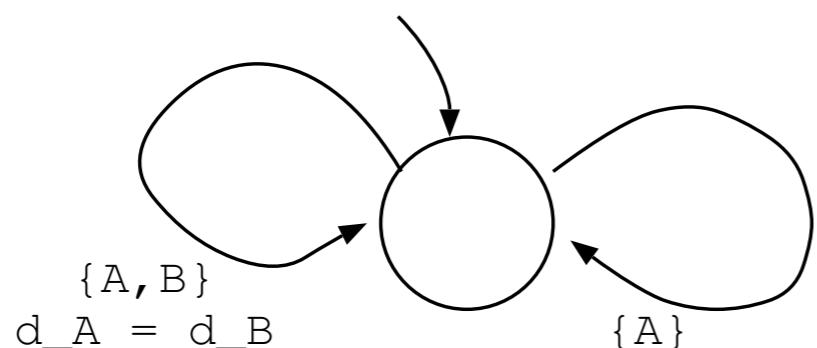
synchronous channel



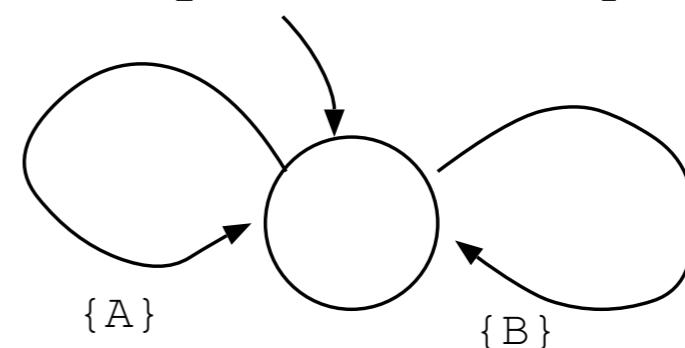
synchronous drain  
or synchronous spout



lossy synchronous channel



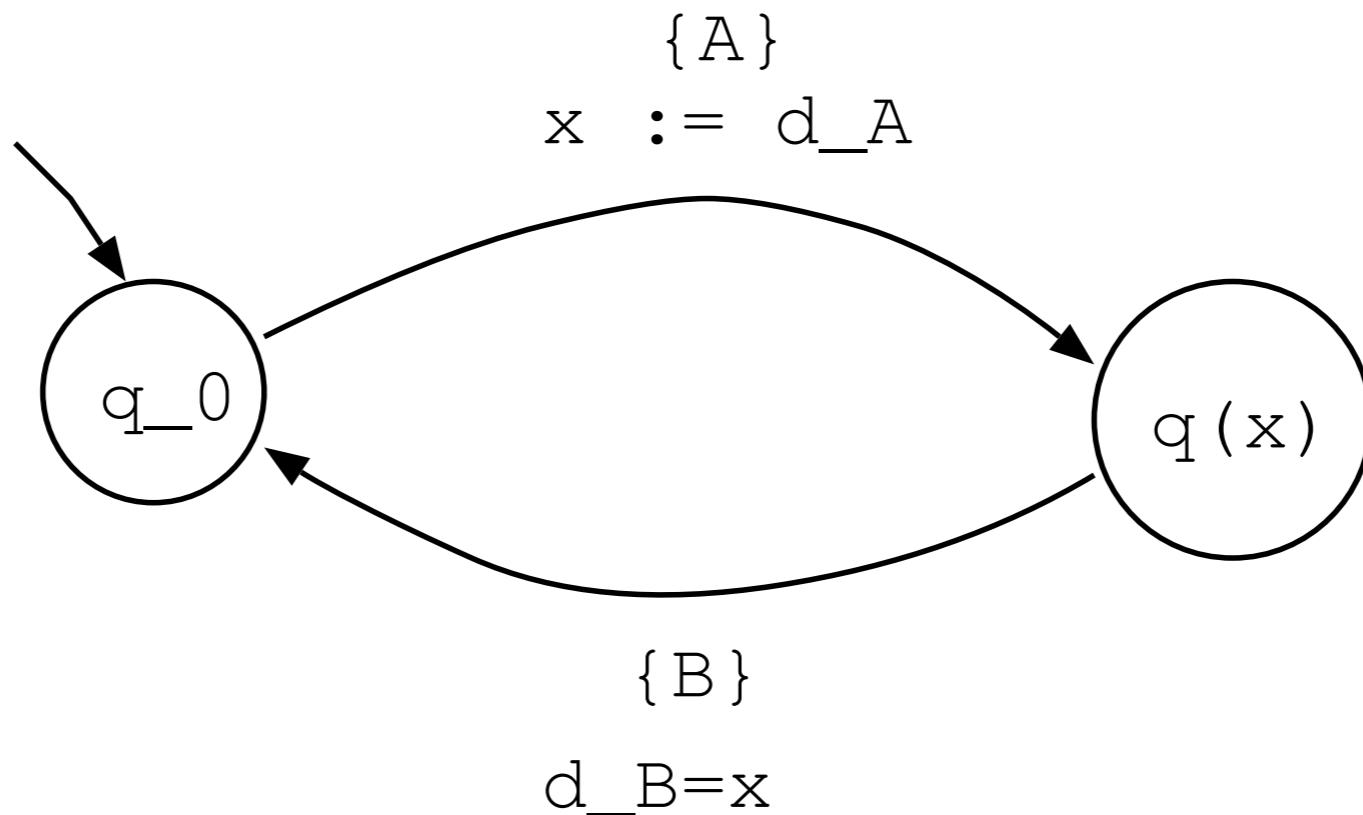
asynchronous drain  
or asynchronous spout



# Parameterised constraint automata

States are parametric on data values ... therefore capturing complex constraint automata emerging from data-dependencies

Example: 1 bounded FIFO



# Composing constraint automata

**Definition 4.1** [*Product-automaton*] The product-automaton of the two constraint automata  $\mathcal{A}_1 = (Q_1, \mathcal{Names}_1, \longrightarrow_1, Q_{0,1})$  and  $\mathcal{A}_2 = (Q_2, \mathcal{Names}_2, \longrightarrow_2, Q_{0,2})$ , is:

$$\mathcal{A}_1 \bowtie \mathcal{A}_2 = (Q_1 \times Q_2, \mathcal{Names}_1 \cup \mathcal{Names}_2, \longrightarrow, Q_{0,1} \times Q_{0,2})$$

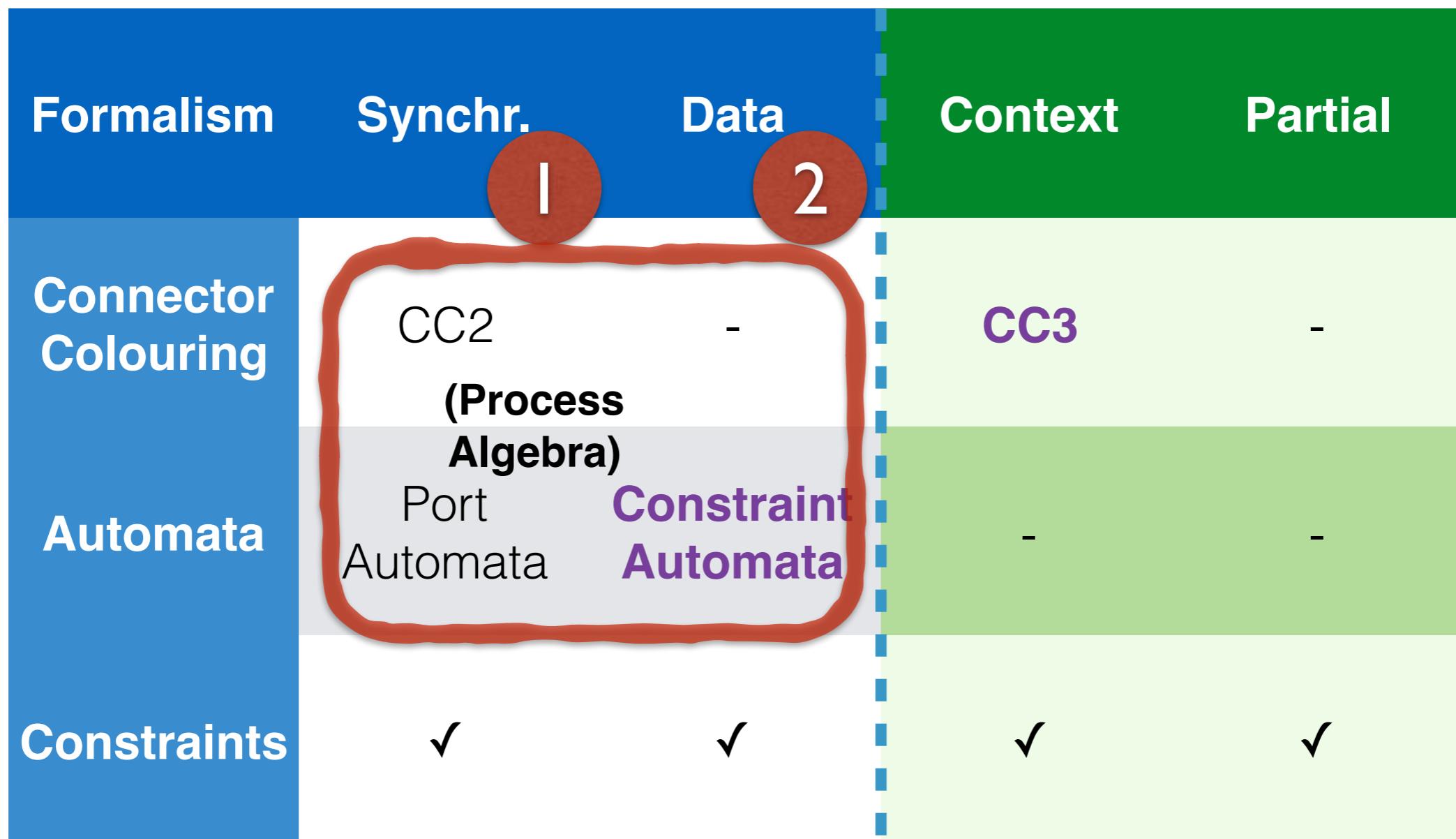
where  $\longrightarrow$  is defined by the following rules:

$$\frac{q_1 \xrightarrow{N_1, g_1} p_1, \quad q_2 \xrightarrow{N_2, g_2} p_2, \quad N_1 \cap \mathcal{Names}_2 = N_2 \cap \mathcal{Names}_1}{\langle q_1, q_2 \rangle \xrightarrow{N_1 \cup N_2, g_1 \wedge g_2} \langle p_1, p_2 \rangle}$$

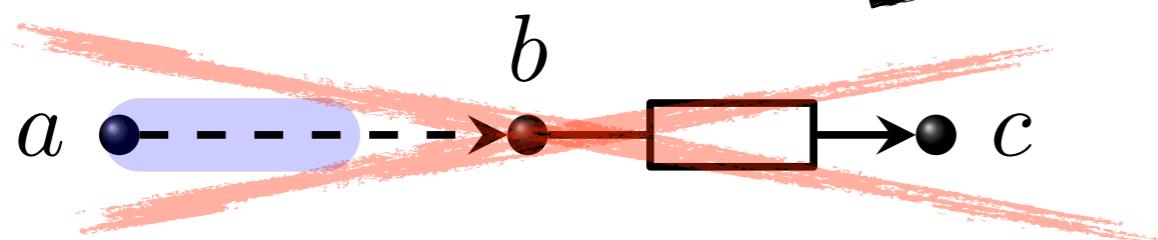
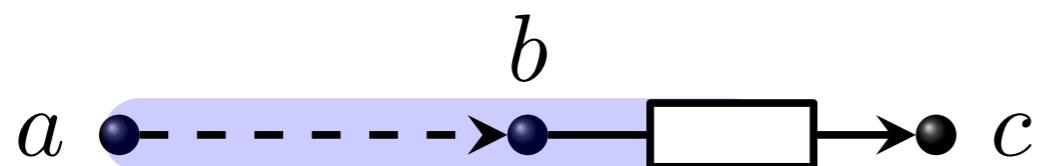
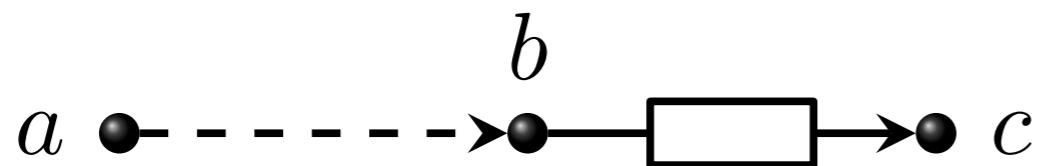
and

$$\frac{q_1 \xrightarrow{N, g} p_1, \quad N \cap \mathcal{Names}_2 = \emptyset}{\langle q_1, q_2 \rangle \xrightarrow{N, g} \langle p_1, q_2 \rangle}$$

# You are here

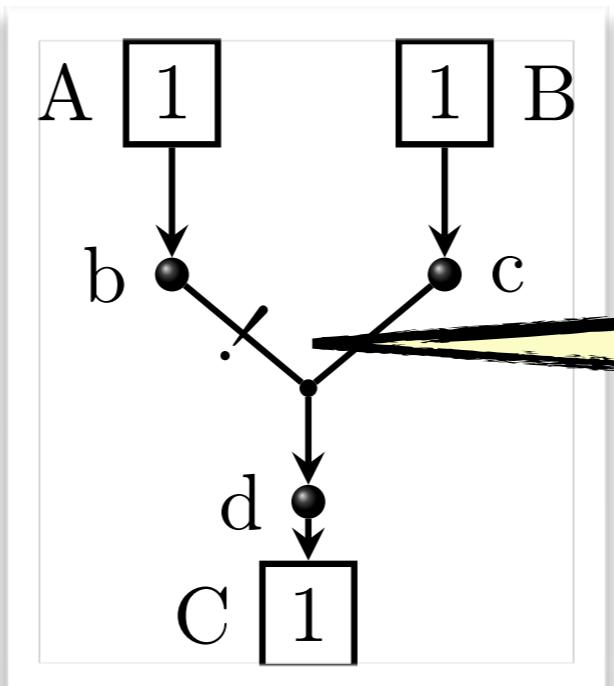


# 2 reasons for context

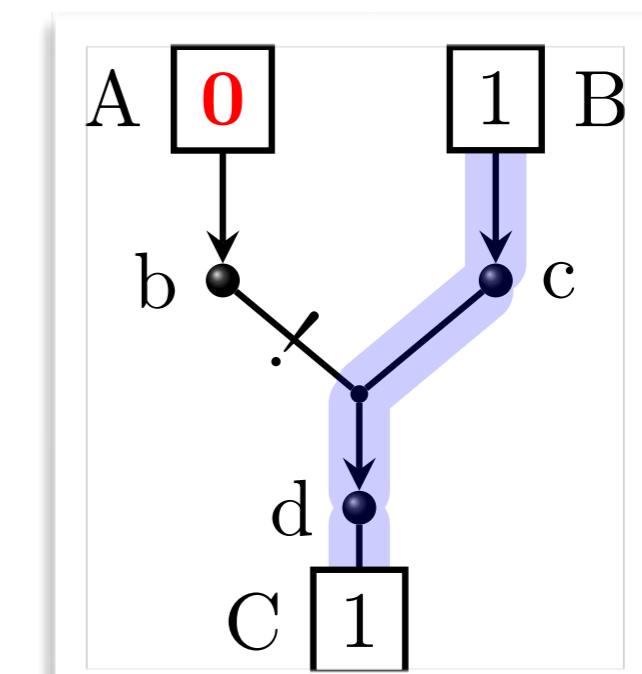
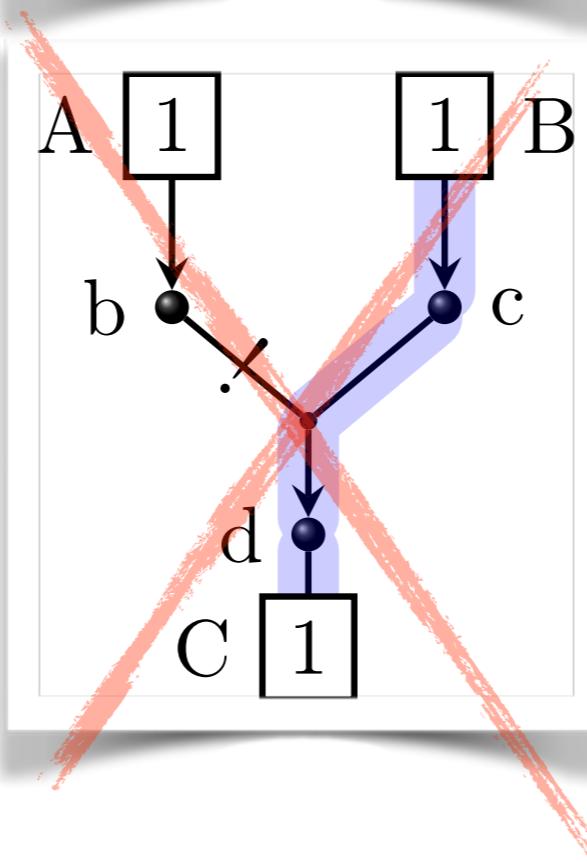
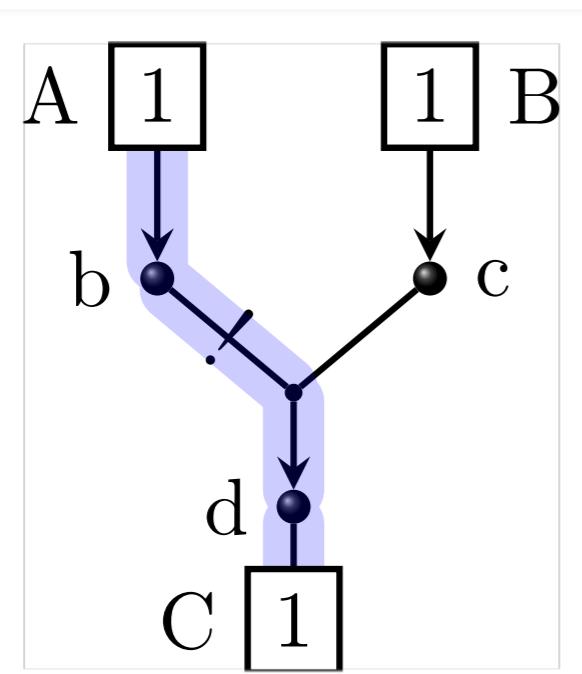


1 - avoid data loss  
when the **context**  
(FIFO) can receive  
the data.

# 2 reasons for context



2 - give **priority**  
based on the  
**context** (writer)

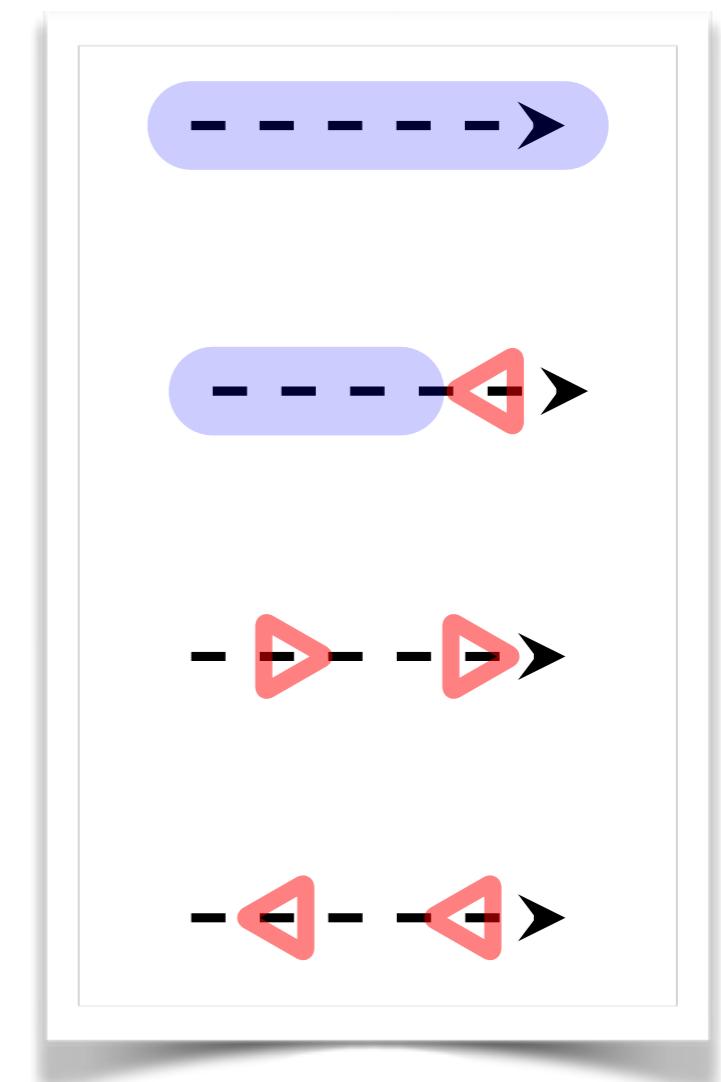
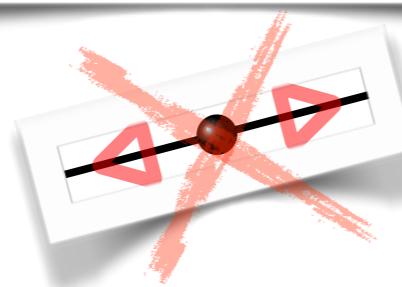
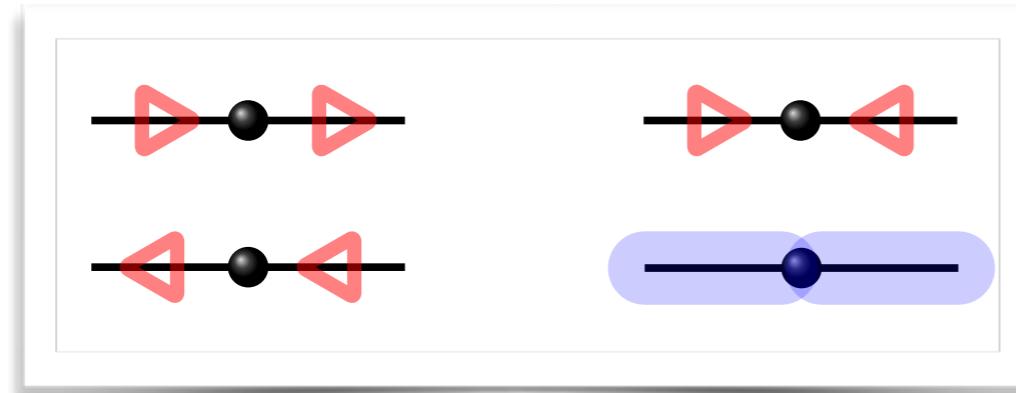


# Context = 3 colours

- *Colouring:*

End → {Flow, GiveReason, GetReason}

- *Composition* = matching colours:



# Context = 3 colours

- *Color*:  $\text{End} = \{e_1, \dots, e_n\} \cup \{\overline{e_1}, \dots, \overline{e_n}\}$

$\text{End} \rightarrow \{\text{Flow}, \text{GiveReason}, \text{GetReason}\}$



- *Composition* = matching colours:



$$CT_1 \bowtie CT_2 =$$

$$\{cl_1 \bowtie cl_2 \mid cl_1 \in CT_1, cl_2 \in CT_2, cl_1 \frown cl_2\}$$

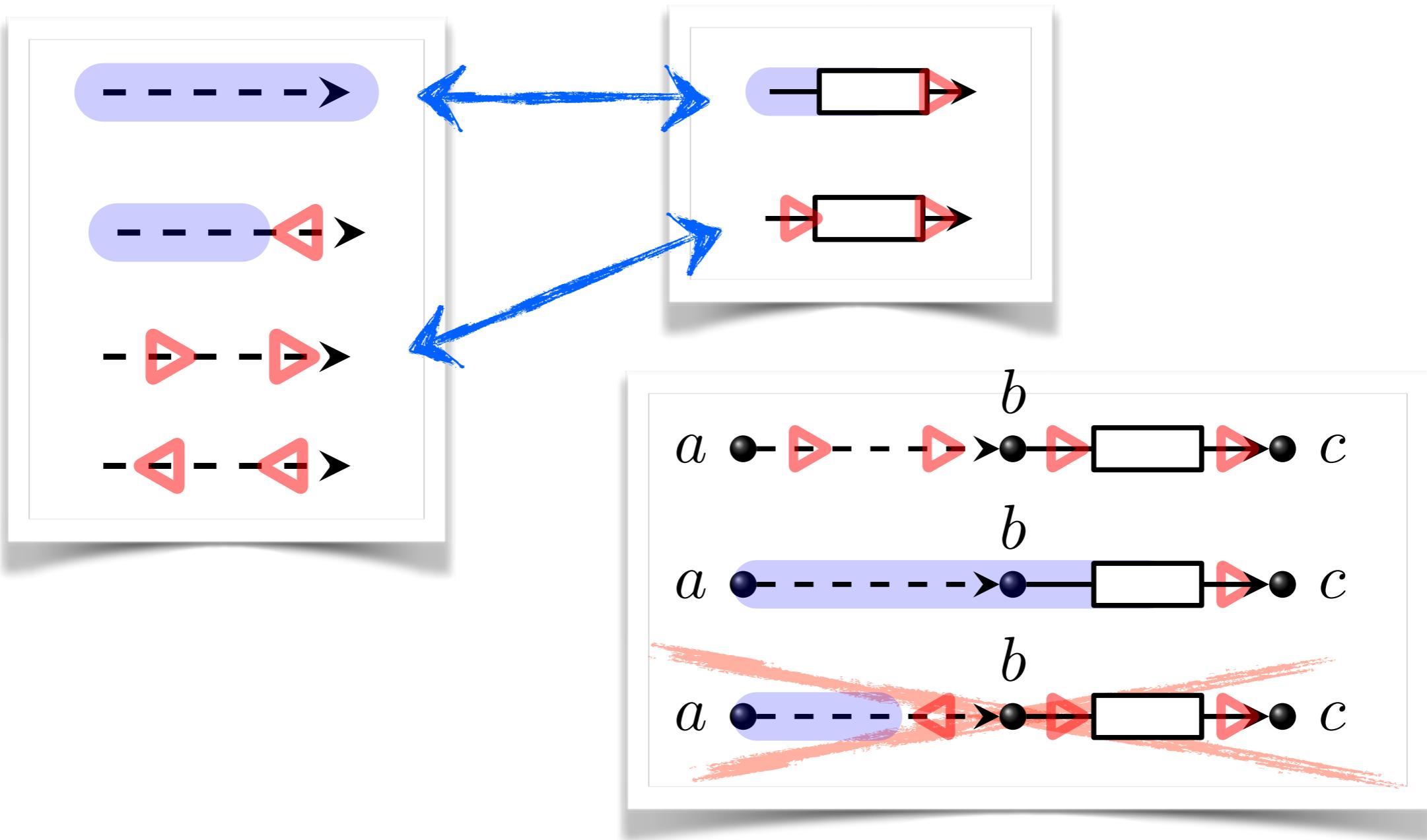
$$cl_1 \frown cl_2 = \forall e_1 \in \text{dom}(cl_1) \cdot \forall e_2 \in \text{dom}(cl_2) \cdot$$

$$e_1 = \bar{e}_2 \Rightarrow$$

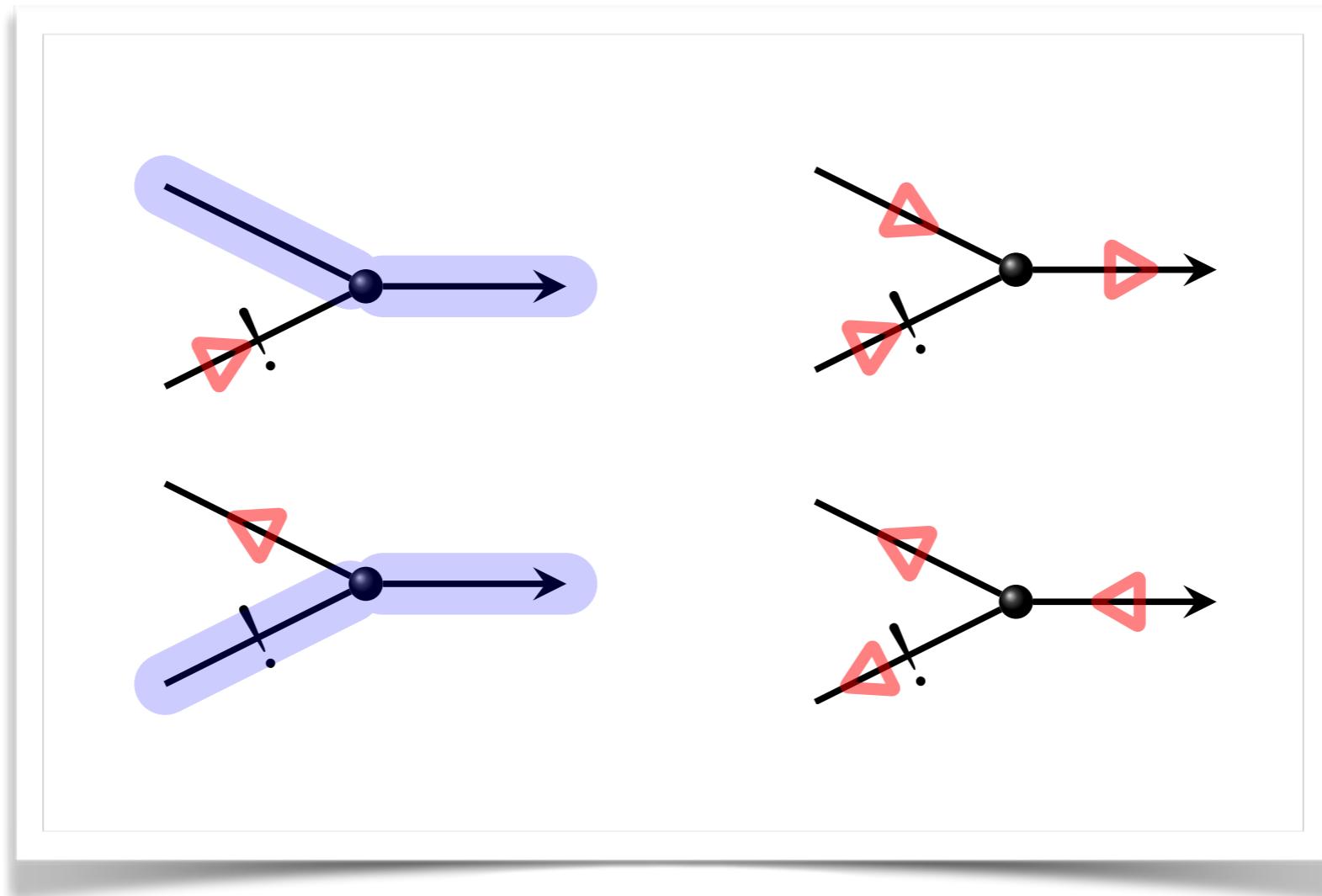
$$(cl_1(e), cl_2(e)) \in \{(\triangleright, \triangleright), (\triangleleft, \triangleleft), (\triangleright, \triangleleft), (\triangleleft, \triangleright)\}$$

$$cl_1 \bowtie cl_2 = cl_1 \cup cl_2$$

# Composition



# Priority with 3 colours



# Connector colouring 3

- **Compositional** – composition operation is associative, commutative, and does not require post-processing.
- Reasons for the absence of flow are **propagated**.
- Expresses **priority**.
- 2 colours  $\Leftrightarrow$  constraint automata (without data)
- 3 colours: + expressive ( $\Leftrightarrow$  intentional automata)

# Build a connector

