Circular Programming Across Paradigms
Proposal for Post-doc Research Project

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1 Summary

We propose to explore the technique of Circular Programming across several programming paradigms. Circular lazy programs, as introduced by Richard Bird, are a famous example that demonstrates the power of a lazy evaluation mechanism. Bird's work showed that any multiple traversal algorithm can be expressed in a lazy language as a single traversal circular function. Using the style of Circular Programming, the programmer does not have to concern him/herself with the definition and the scheduling of the different traversal functions, since a single (traversal) function has to be defined. Moreover, because there is a single traversal function, the programmer does not have to define intermediate gluing data structures to convey values computed in one traversal and needed in following ones, either.

In our work, we intend to systematically explore the nice of circular programs in programming paradigms such as bidirectional transformations, incremental computing, program calculation, attribute grammars or spreadsheets.

2 The Team

2.1 Post-doc Researcher

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João Fernandes will obtain his PhD. title in Computer Science from the University of Minho in ? ?. The title of his PhD. thesis is *Design, Implementation and Calculation of Circular Programs*. His promotor and co-promotor are Prof. Dr. João Saraiva (Universidade do Minho), and Prof. Dr. Oege de Moor (Oxford University).

2.2 Supervisors

> Prof. Dr. Alberto Pardo
> Instituto de Computación
> Universidad de la República
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Alberto Pardo is Associate Professor of the Instituto de Computación (INCO) at Universidad de la Repblica (Montevideo, Uruguay), which he joined in 1986, and the head of the Formal Methods Group of INCO. He also taught Computer Science courses at Universidade Federal de Pernambuco (Brazil) and Technische Universität Darmstadt (Germany). Alberto Pardo holds an M.Sc. degree from the Universidade Federal de Pernambuco and a PhD from the Technische Universität Darmstadt. His research interests are focused on program transformation techniques for functional programs, generic programming and formal semantics of programming languages.

Alberto Pardo has been responsible for several research projects on program transformation tecniques in subjects close to this project. He is member of the IFIP TC2 Working Group 2.1 on "Algorithmic Languages and Calculi". He has also been involved in the organization of various international events like, for example, the International Summer School on Language Engineering and Rigurous Software Development (LERNET 2008), the 11th International Conference on Logic for Programming Artificial Intelligence and Reasoning (LPAR 2004), and the International Winter School on Semantics and Applications (WSSA 2003).

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João Saraiva is an university lecturer of Computer Science at University of Minho and the research coordinator of the Department of Informatics in the Algoritmi Research Institute. His research is focused on programming language design and implementation, and functional programming. João Saraiva completed a Ph.D. program at Utrecht University, The Netherlands, in December 1999 where he worked on purely functional implementation of attribute grammars.

João Saraiva has been involved in the organization of various international events in the context of this project, for example, the 10th European Joint Conferences on Theory and Practice of Software (ETAPS 2007), the International Summer Schools on Advanced Functional Programming AFP'98 (Swierstra et al., 1999b), Applied Semantics APPSEM'00 (Barthe et al., 2002) and Generative and Transformation Techniques on Sofware Enginnering 2005, 2007 and 2009 (Lämmel et al., 2006), and the International Workshop on Attribute Grammars and their Applications (WAGA) and International Workshop on Language Descriptions Tools and Application (LDTA).

2.3 Host Institutions

This Pos-doc research project will be carried out in the Department of Informatics at Minho University. Several members of the department (José Nuno Oliveira, Luís Barbosa, José Barros, Jorge Sousa Pinto, João Saraiva) are investigating the use of formal methods and generic programming in the context of Program Understanding and Re-engineering.

Programming languages, design and implementation is also an intensive area of research in the department (Pedro Henriques, José Almeida, José Ramalho, João Saraiva). Work in this area has been done around the Lrc project in collaboration with Ordina Research, Holland (Dr. Matthijs Kuiper) and the group on Software Technology of the Department of Computer Science at Utrecht University (headed by Prof. Dr. Doaitse Swierstra), and we keep in regular contact with our industrial and academic collaborators.

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3 Introduction/Motivation

Circular lazy programs, as introduced by Bird (1984), are a famous example that demonstrates the power of a lazy evaluation mechanism. Bird's work showed that any multiple traversal algorithm can be expressed in a lazy language as a single traversal *circular function*. Such a (virtual) circular function may contain a *circular definition*, that is, an argument of a function call that is also a result of that same call. Although circular definitions induce non-termination under a strict evaluation mechanism, they can be immediately evaluated using a lazy evaluation strategy. The lazy engine is able to compute the right evaluation order, if that order exists. Indeed, using this style of circular programming, the programmer does not have to concern him/herself with the definition and the scheduling of the different traversal functions, since a single (traversal) function has to be defined. Moreover, because there is a single traversal function,

the programmer does not have to define intermediate gluing data structures to convey values computed in one traversal and needed in following ones, either.

Bird's work showed the power of circular programming, not only as an optimization technique to eliminate multiple traversal of data, but also as a powerful, elegant and concise technique to express multiple traversal algorithms. Circular programs are also used in the construction of Haskell compilers (Marlow and Jones, 1999; Hinze and Jeuring, 2002), to express pretty printing algorithms (Swierstra et al., 1999a), breadth-first traversal strategies (Okasaki, 2000), type systems (Dijkstra and Swierstra, 2004) and aspect-oriented compilers (de Moor et al., 2000). As an optimization technique, circular programs are used, for example, in the deforestation of accumulating parameters (Voigtländer, 2004). Circular programs can also be obtained through partial evaluation (Lawall, 2001) and continuations (Danvy and Goldberg, 2002).

4 Tasks

In this section we present the different working directions that compose our reserach proposal. All of them have circular programming as the common component.

4.1 Strictification of Circular Programs in Calculational Form

Functional programs often combine separate parts of the program using intermediate structures for communicating results. Programs such as $prog = cons \circ prod$, where $prod$ is called the producer function and $cons$ is called the consumer function, are modular and have many benefits, such as clarity and maintainability, but suffer from inefficiencies caused by the generation of the intermediate data structures that glue functions $cons$ and $prod$ together.

Indeed, the elimination of such intermediate structures, also called program fusion, is a key aspect taken into account in the implementation of functional compilers (Jones et al., 1993; Leroy, 1997). Program fusion has, therefore, been thoroughly studied in the context of functional languages: for pure programs (Wadler, 1990; Gill et al., 1993; Onoue et al., 1997; Ohori and Sasano, 2007; Fernandes et al., 2007) but also in the context of monadic programs (Ghani and Johann, 2008; Manzino and Pardo, 2008; Pardo et al., 2009).

Another key optimization to implement in compilers for lazy languages such as *Haskell* is the static detection of functions that can be evaluated strictly. Indeed, an important area of research is strictness analysis (**?**). Thus, we plan to study how to transform circular programs into strict ones, using calculational techniques and proving the correctness of the transformation. In this research, we will closely follow the approach studied in (Fernandes and Saraiva, 2007), where attribute grammar techniques have been adapted to transform circular programs into compositions of strict programs. The correctness of such techniques, however, remains to be formally proved.

In order to be able to calculate strict programs from circular ones, we initially will try to invert the transformation presented in (Fernandes et al., 2007): there, a calculation rule was proposed to calculate circular programs from strict ones.

4.2 Bidirectional Transformations

There are many situations in which one data structure, called *source*, is transformed to another, called *view*, in such a way that changes on the view can be transformed back to those on the original data structure. This is called Bidirectional Transformation (BT), and pratical examples include synchronization of replicated data in different formats (Foster et al., 2005), presentation-oriented structured document development (Hu et al., 2004; Michiel, 2004), interactive user interface design (Meertens, 1998), and the well-known view updating mechanism which has been intensively studied in the database community (Bancilhon and Spyratos, 1981; Dayal and Bernstein, 1982; Gottlob et al., 1988; Lechtenbörger and Vossen, 2003). The simple diagram presented below illustrates a Bidirectional Transformation.
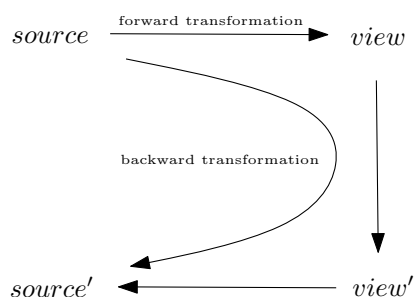
Figure 1: Bidirectional Transformation

It was during a visit of the candidate to one of the leading research groups in the area of Bidirectional Transformation, at the University of Tokyo, that it was preliminary discussed how such transformations could benefit from the properties of circular programs. Indeed, circular programs may provide an ideal setting to compute a new *source*, given the original one and it's *view*, but submitted to a particular change.

In this task, we intend to fully explore this promising research direction. Our plan is to formally establish how circular programs can be integrated within Bidirectional Transformations, namely how circular programs can be used in the backward transformation of BTs.

4.3 Incremental Computation

Incremental computation is about maintaining the input-output relationship of a program, as the input undergoes changes. The changes in the input may be such that one cannot avoid a complete recomputation of the output. However, in many cases, one can reuse results of the previous computation to update the output more efficiently than by performing a complete recomputation from scratch. Obviously, incremental computation is more efficient for cases where changes in the input cause small changes in the output.

The investigation field of incremental computation has proven to be an exciting one, as, over the years, several researchers have studied and proposed techniques to reuse previously computed results, in order to improve efficiency of

computer programs. Incremental Computation is, indeed, essential to the implementation of programming environments (Reps and Teitelbaum, 1989; Michiel, 2004) or spreadsheets, for example.

Change Propagation (Reps, 1982), Adaptive Programming (Acar et al., 2002, 2006b,a) and Function Memoization (Pugh and Teitelbaum, 1989; Hughes, 1985) are among the techniques proposed to achieve Incremental Computation.

However, the Change Propagation and Function Memoization approaches do not handle circular programs. Furthermore, Reps' techniques do not handle circular attribute grammars. Thus, the incremental functional implementations derived from incremental attribute grammars will never be circular programs.

Acar's ingenious Adaptive Programming technique is proposed in the strict functional setting ML and its implementation in Haskell (Carlsson, 2002) does not support *lazyness*. Thus, his technique also does not allow to combine incrementality with the circular definitions that may occur in a *lazy* setting.

As for Memoization, Hughes' *lazy* memo-functions are specially suitable to manipulate circular (infinite) structures. However, these circularities are not of the same kind as the ones we want to be able to deal with: we exploit the use of function call results as some of the same call arguments with the purpose of eliminating multiple traversals over data structures. It is still not clear how to memoize such circular function calls.

Our plan in this subject is the development of techniques that make it possible to combine incrementality with circular programming.

4.4 Attribute Grammars

Circular programs and Attribute Grammars are closely related. Indeed, as Johnsson (1987) and Swierstra and Kuiper (Kuiper and Swierstra, 1987) originally showed, circular programs are the natural representation of attribute grammars in a lazy setting (Swierstra and Azero, 1998; de Moor et al., 2000; Saraiva, 1999; Dijkstra, 2005). Furthermore, several *Haskell* and circular based Attriubte Grammar Systems have been developed (Swierstra et al.; Wyk et al., 2006).

In our research, we plan to use circular program strictification techniques, in the sense described in Section 4.1, to derive/design a correct by construction Attribute Grammar System. Furthermore, we plan to incorporate in such a system our developments on Incremental Computation, as described in Section 4.3, in order to obtain incremental attribute evaluators. Indeed, incremental evaluators are an important application of Attribute Grammars after the seminal work of Tom Reps on the Synthesizer Generator system(Reps and Teitelbaum, 1989).

4.5 Spreadsheets

Spreadsheet tools can be viewed as programming environments for non-professional programmers. These so-called "end-user" programmers vastly outnumber professional programmers. In fact, spreadsheets, when viewed as a programming language (PL), are one of the largest PLs and can be characterized as a particularly low-level one: there is no support for abstraction, testing, encapsulation, or structured programming. As a result, numerous studies have shown that existing spreadsheets contain errors at an alarmingly high rate.

Surprisingly, there is little work by the programming language community on the foundations of spreadsheets, being the works (Burnett, 2004; Abraham et al., 2005; Erwig et al., 2005) an exception.

Spreadsheets are the motivating example for incremental evaluation. Indeed, a spreadsheet defines dependencies between different cells. When the user changes the value of one cell, only the ones that are affected by the change are re-evaluated.

Building a spreadsheet system is a complex and hard-working task: the developer has to define/maintain not only a complex dependency graph to determine the re-evaluation order and propagate changes, but also a powerful incremental evaluation engine. Within the style of circular programming the user does not have to handle such dependencies: the lazy machinery infers the dependencies and evaluation order at runtime. Moreover, if we combine circular programming with incremental evaluation, then we have a perfect setting to develop spreadsheets.

4.6 Research Questions

With our work, we plan to answer the following questions:

- how can circular programs be transformed, in a calculational setting, into strict programs, whose execution is not restricted to a lazy execution model? A calculational setting is essential since we want to be able to prove the correctness of the transformation.

- develop a proved correct Attribute Grammar System, once we have the answer to the previous research question. Indeed, by then we will be able to prove that the transformations implemented in such system are correct.

- how to fully explore circular definitions in the implementation of Bidirectional Transformations? In particular, up to which extent can circular programs be used in the implementation of simple and concise backward transformations?

- how can the nice properties of circular programming be combined with incremental programming? Ideally, we intend to develop a framework where we can write circular programs that can be executed incrementally.

- implement a spreadsheet system, using our circular and incremental programming setting. Such a programming environment is indeed the ideal one to avoid the complex tasks of maintaining all the dependencies between all the cells of a spreadsheet and of determining a re-evaluation order to propagate the changes resulting from a change in a cell.

4.6.1 Significance

This proposal is geared towards realizing the full potential of circular programming, by exploring its best properties in the interest of a wide range of programming/research areas. We expect benefits of performance, conciseness, and robustness in areas such as program calculation, bidirectional transformations or spreadsheets, for example.

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