Verifiable Side-Channel Security of Cryptographic Implementations: Constant-Time MEE-CBC.

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Breaking that Title Down

Our main practical contribution: A *machine-checked* proof of IND\$-CPA and INT-PTXT security for x86 code implementing *MAC-then-Encode-then-CBC-Encrypt* (MEE-CBC) against some *timing adversaries*.

- Why MEE-CBC? Simple crypto, but very difficult to implement securely.
- Why machine-checked? Necessary to take implementation details into account, and verify implementations for properties not easily testable...
- Such as their timing behaviour, which has been exploited in the past to break MEE-CBC. We show a new attack on AWS Labs's implementation of MEE-CBC in s2n.

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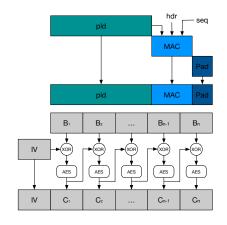
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MEE-CBC: An Overview



- ▶ Payload is fed through MAC with additional data;
- Payload and tag are concatenated and padded to multiple of block length;
- ► The result is fed through AES-CBC.

On the Side-Channel Security of MEE-CBC

When decrypting:

- Length of padding must be known to check the MAC;
- ► Padding validity needs to be checked.

The problem: AES-CBC provides only CPA security.

▶ Decrypted ciphertext is sensitive until MAC has been checked.

Countermeasures and attacks:

- Both padding and MAC computation must be performed always [Vaudenay, 2002];
- Number of compression function queries in MAC computation must be independent from padding length or validity [AlFardan and Paterson, 2013];

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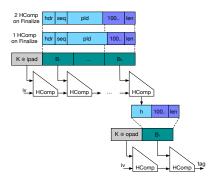
Countermeasures in Practice

- ► After Lucky Thirteen [AlFardan and Paterson, 2013], many switch to "constant-time" programming policy.
 - No secret-dependent branching (prevents coarse leaks via overall execution time, some leaks via branch prediction);
 - No secret-dependent memory accesses (prevents precise leakage via cache timing).
- ▶ In s2n, AWS Labs do limited mitigation in MEE-CBC and hide whatever leakage is left behind a random delay.
 - Randomization is insufficient in practice [Albrecht and Paterson, 2016];
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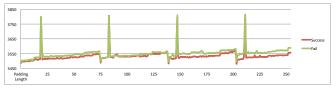
HMAC and s2n's Additional Mitigation



- Mitigation aimed at better balancing number of compression function calls.
- ► Finalize call for inner hash may make 1 or 2 compression queries depending on length of final message block;
- 9 bytes are reserved for SHA-X padding (8 payload length bytes + 1 0x80 byte).

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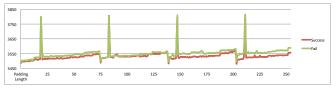
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Black-box specification security usual notion of provable security;

Functional correctness of implementation: the input-output

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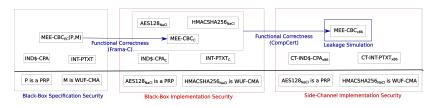
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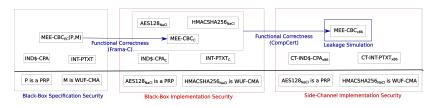
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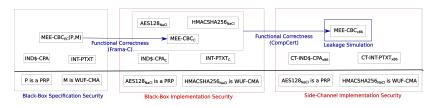
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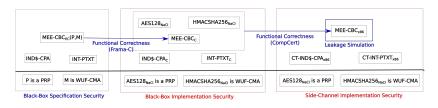
- ▶ We formalize a black-box security proof in EasyCrypt.
- We prove equivalence of a new C implementation of MEE-CBC to a functional spec extracted from EasyCry
 - EasyCrypt specification is generic in block and tag lengths and (length-regular and invertible) padding function.
 - We instantiate it with relevant values (and discharge proofs) before extraction.
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Black-Box Specification Security Formally

- ▶ We also prove some weak length hiding.
 - Not shown here: we don't transfer it to implementation.

Side-Channel Implementation Security Formally

- ▶ Applies to implementations of the primitive in a language \mathcal{L} ...
- ▶ ... whose leaky semantics are animated by a machine M.
- ▶ We use the same M as [Barthe et al., 2014]:
 - language is x86,
 - semantics are those of CompCert,
 - leakage trace reveals ordered sequence of branching operations and memory accesses.

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 \begin{array}{c} \textbf{Game } \mathbb{M}\text{-IND\$-CPA}^{\mathcal{A}}_{\Pi^*,\phi}(b) \colon \\ \hline key \overset{\$}{\leftarrow} \mathbb{M}(\mathsf{Gen}^*)_{\leadsto \ell_g} \\ b' \overset{\$}{\leftarrow} \mathcal{A}^{\mathsf{RoR}} \overset{\mathsf{Decrypt}}{\leftarrow}(\ell_g) \\ \mathsf{Return} \ (b' = b) \\ \hline \end{array} \quad \begin{array}{c} \mathbf{proc.} \ \mathsf{RoR}(\mathbf{m}) \colon \\ \hline c \overset{\$}{\leftarrow} \mathbb{M}(\mathsf{Enc}^*,\mathsf{m},\mathsf{key})_{\leadsto \ell_e} \\ \\ \mathsf{If} \ (b = \mathsf{Ideal}) \ \mathsf{Then} \ c \overset{\$}{\leftarrow} \{0,1\}^{|\mathsf{m}|} \\ \\ \mathsf{Return} \ (c,\ell_e) \\ \hline \mathbf{proc.} \ \mathbf{Dec}(\mathbf{c}) \colon \\ \hline \mathbf{m} \leftarrow \mathbb{M}(\mathsf{Dec}^*,\mathsf{c},\mathsf{key})_{\leadsto \ell_d} \\ \\ \mathsf{Return} \ (\bot,\ell_d) \\ \end{array}
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Total Functional Correctness Formally

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- ► Captures perfect (rather than probabilistic) correctness.
 - Prevents algorithm substitution attacks IF the property can be checked before running.
 - Some weakening may be possible if a proof of resilience against ASA exists on the specification.
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ightharpoonup au_{alg} is determined by the black-box security experiment for each algorithm:

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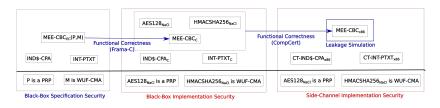
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BAck to application to MEE-CBC



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Performance

Implementation	Compiler	Time
s2n	GCC -02	5μ s
OpenSSL	GCC -O2	9μ s
MEE-CBC _C (AES-NI)	CompCert*	21μ s
MEE-CBC _C	GCC -O2	25ms
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MEE-CBC _{x86}	CompCert	42ms
MEE-CBC _C	GCC -O0	99ms

- ► Time taken to decrypt a 1.5kB TLS record.
- ▶ A very large part of the cost is due to constant-time AES.
 - Vector instructions not supported by CompCert
 - AES-NI gives reasonable results even with modified CompCert
 - But not all proofs have been adapted
- ► Some is due to CompCert (typically ca. 2× w.r.t. GCC -O2).
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Summary

- ► Some formal guarantees can be obtained in realistic settings.
- We propose a framework that breaks the problem down into more manageable parts, essentially by successive refinements.
- ► There is still a cost to pay for formal guarantees.
- ► In proof effort:
 - in practice, most effort expended in top two levels;
 - twisting the implementation to guarantee leakage simulation makes it harder to verify functional correctness.
- ► In performance:
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► Modular trust:

- Trust [Paterson, Ristenpart and Shrimpton, 2011]? Get black-box LH-AEAD and side-channel INT-CTXT for free on the compiled code.
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Questions?